

# Unbound exotic nuclei studied by projectile fragmentation.

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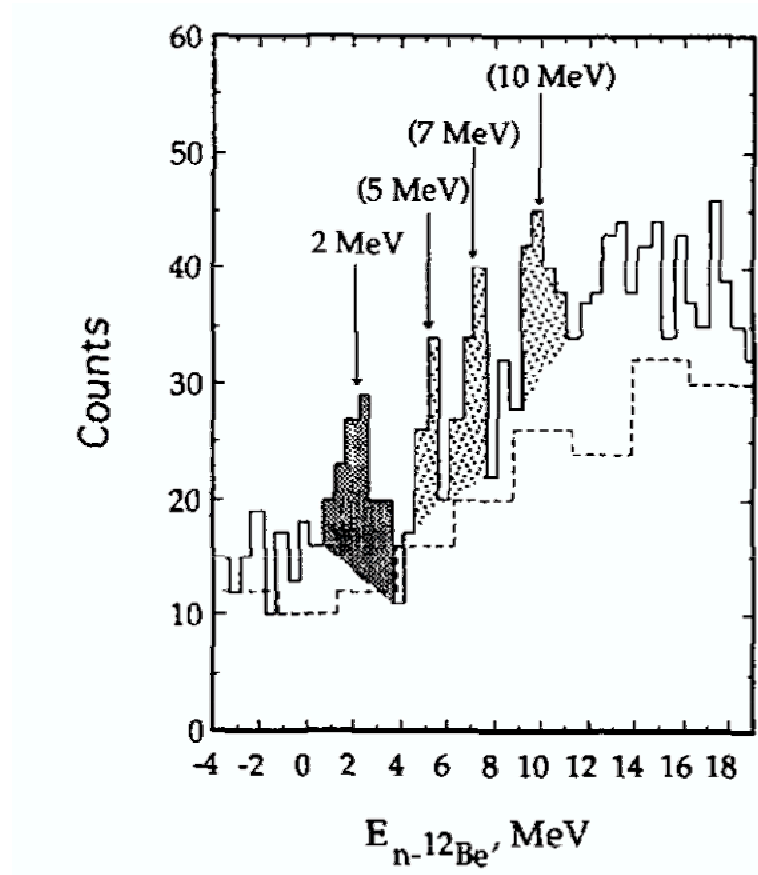
## Outline.

- Reactions to study  $^{13}\text{Be}$  .
- Simple time dependent model for the excitation of a nucleon from a bound state to a continuum resonant state.
- Conclusion and Outlooks.

## Reactions to study halo nuclei.

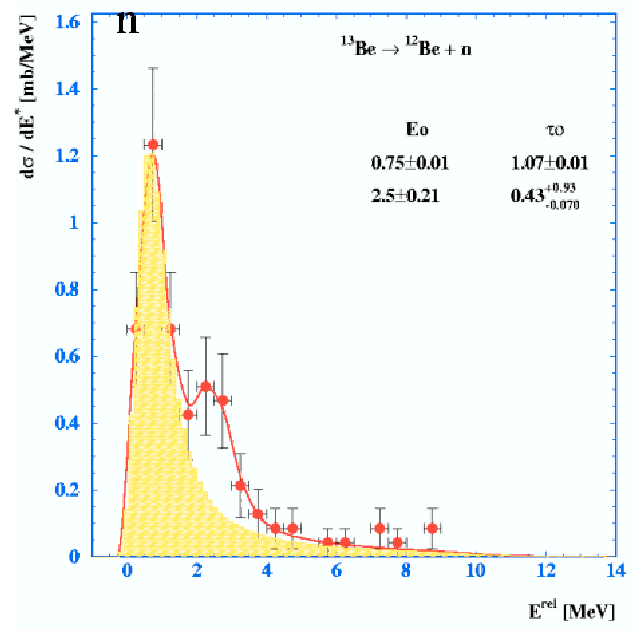
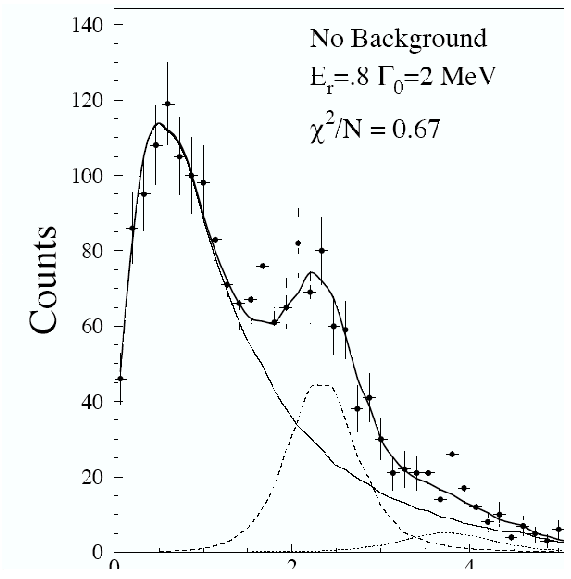
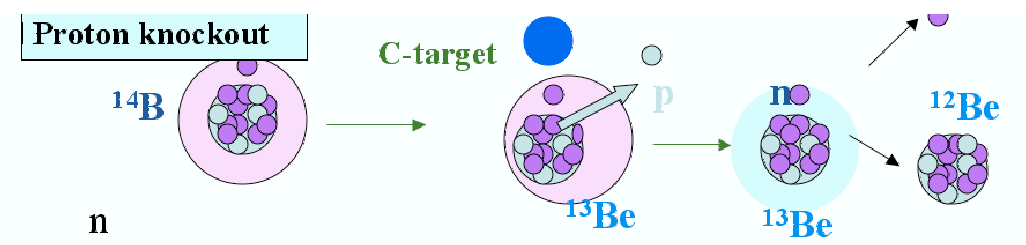
- Transfer to the continuum reaction.
- Fragmentation reaction.

# $^{13}\text{Be}$ obtained by transfer reaction



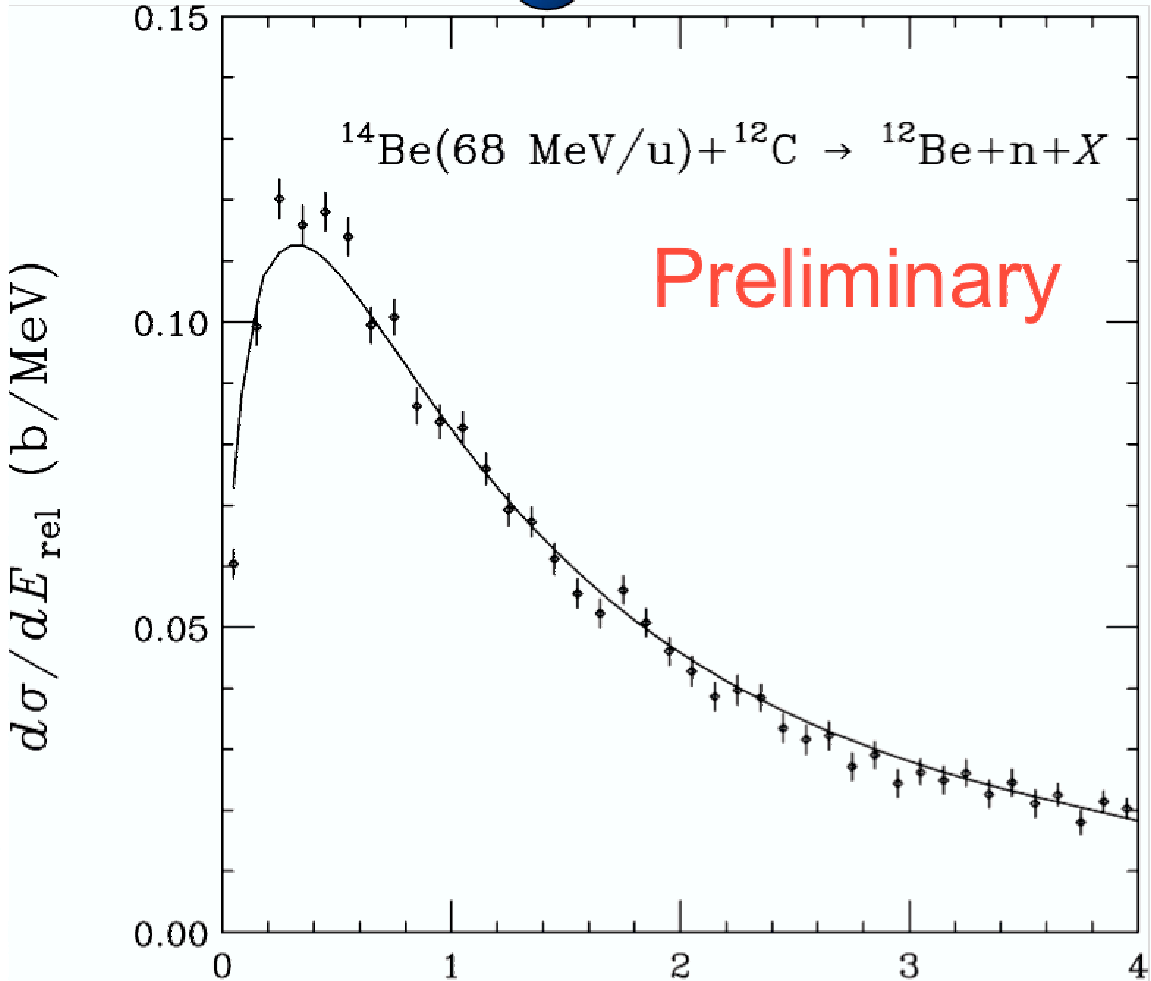
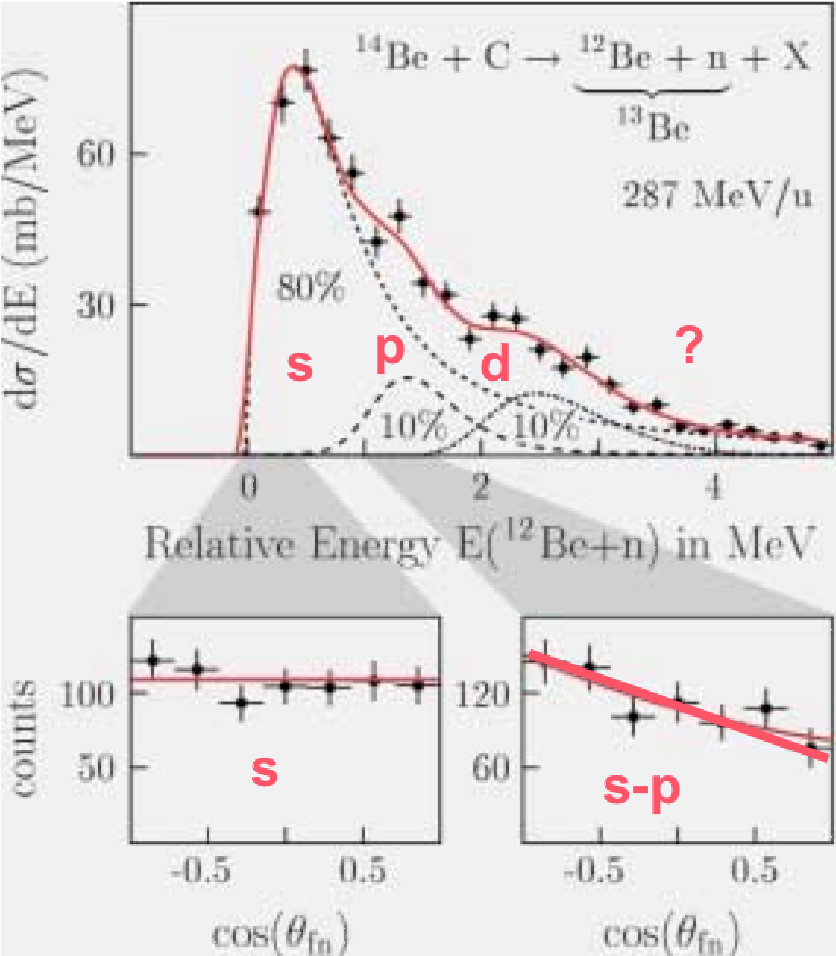
$^{12}\text{Be}$  (d,p) RIKEN (Korshennikov) (1995)

# $^{13}\text{Be}$ obtained by proton knockout on $^{14}\text{B}$



(a) LPC GANIL (Lecouey, Orr) (2002). (b) GSI (U Datta Pramanik) (Surrey conference Jan.2005).

# $^{13}\text{Be}$ obtained by neutron knockout from $^{14}\text{Be}$



(a) GSI (Simon Nucl. Phys. A734 (2004) 323-326, (b) RIKEN (Nakamura)(ECT\* 2004)unpublished

## Inelastic excitation.

Inelastic-like excitations can be described by the first order time dependent perturbation theory amplitude:

$$A_{fi} = \frac{1}{i\hbar} \int_{-\infty}^{\infty} dt \langle \psi_f(t) | V_2(\mathbf{r}) | \psi_i(t) \rangle$$

In order to obtain a simple analytical formula we consider the special case in which  $V_2(r) = v_2 \delta(x) \delta(y) \delta(z)$ .

$$A_{fi} = \frac{v_2}{i\hbar v} \int_{-\infty}^{\infty} dz \psi_f^*(b_c, 0, z) \psi_i(b_c, 0, z) e^{iqz}$$

## General wave functions (asymptotic form)

For the initial state:

$$\psi_i(b_c, 0, z) = -C_i i^l \gamma h_{l_i}^{(1)}(i\gamma r) P_{l_i}(z/r).$$

For the final continuum state:

$$\psi_f(b_c, 0, z) = C_f k \frac{i}{2} (h_{l_f}^{(+)}(kr) - S_{l_f} h_{l_f}^{(-)}(kr)) P_{l_f}(z/r).$$



## Simple time dependent modele.

$$A_{fi} = \frac{v_2}{i\hbar v} \int_{-\infty}^{\infty} dz \psi_f^*(b_c, 0, z) \psi_i(b_c, 0, z) e^{iqz}$$

$$I(k, q) = I_R + iI_I = |I|e^{i\alpha}$$

$$\bar{S} = S e^{2i\alpha} = e^{2i(\delta + \alpha)}$$

$$|A_{fi}|^2 = C^2 |I|^2 |1 - \bar{S}|^2.$$

## Comparison to the transfer to the continuum.

Fragmentation:

$$\frac{dP_{in}}{d\varepsilon_f} = \frac{2}{\pi} \frac{v_2^2}{\hbar^2 v^2} C_i^2 \frac{m}{\hbar^2 k} \sum_{l_f} (2l_f + 1) |1 - \bar{S}_{l_f}|^2 |I_{l_f}|^2.$$

Transfer:

$$\frac{dP_t(b_c)}{d\varepsilon_f} \approx \frac{4\pi}{k^2} \sum_{l_f} (2l_f + 1) |1 - S_{l_f}|^2 B_{l_f, l_i}$$

(*G. Blanchon, A. Bonaccorso and N. Vinh Mau, Nucl. Phys. A739 (2004) 259.*)

## Cross section.

$$\frac{d\sigma}{d\varepsilon_f} = C^2 S \int_0^\infty d\mathbf{b}_c \frac{dP_{in}(b_c)}{d\varepsilon_f} P_{ct}(b_c),$$

The core survival probability:

$$P_{ct}(b_c) = |S_{ct}|^2$$

$$P_{ct}(b_c) = e^{(-\ln 2 \exp[(R_s - b_c)/a])}$$

## Determination of the S-matrix.

$$h = t + U.$$

$$U(r) = V_{WS} + \delta V.$$

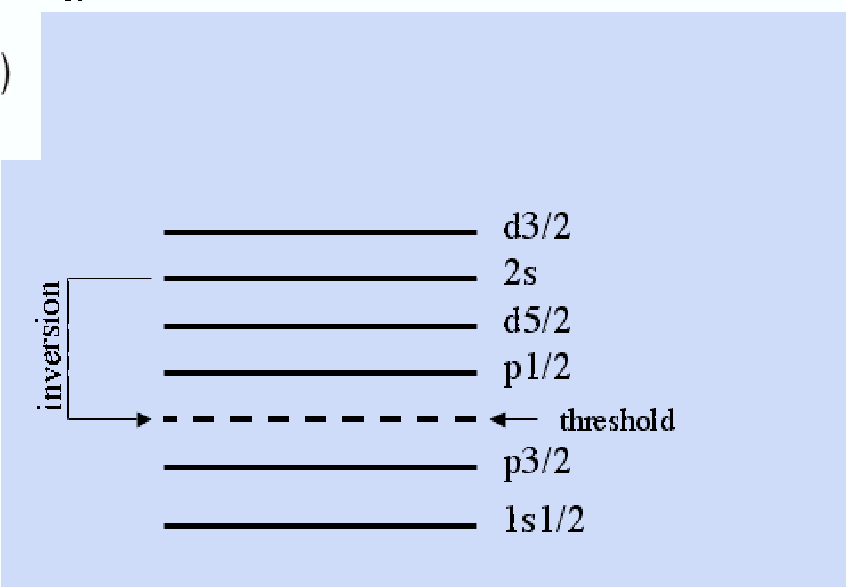
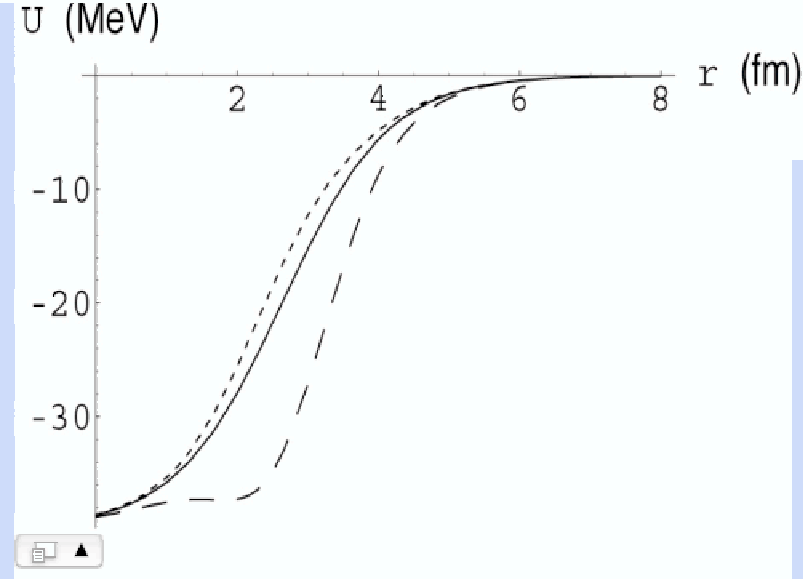
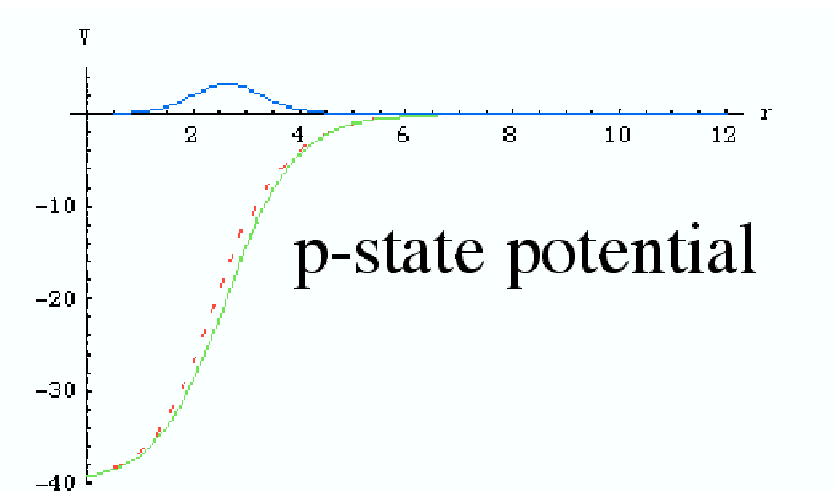
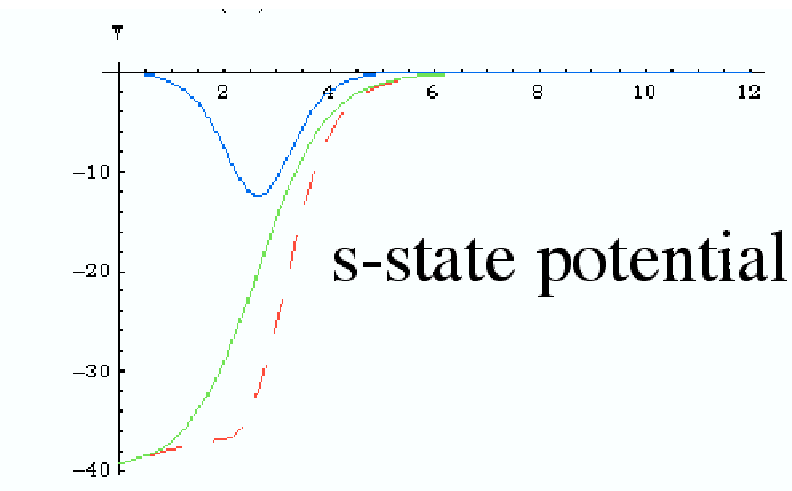
$$\delta V(r) = 16\alpha e^{2(r-R)/a} / (1 + e^{(r-R)/a})^4.$$

$V_{WS}$  = Woods-Saxon potential plus spin-orbit.

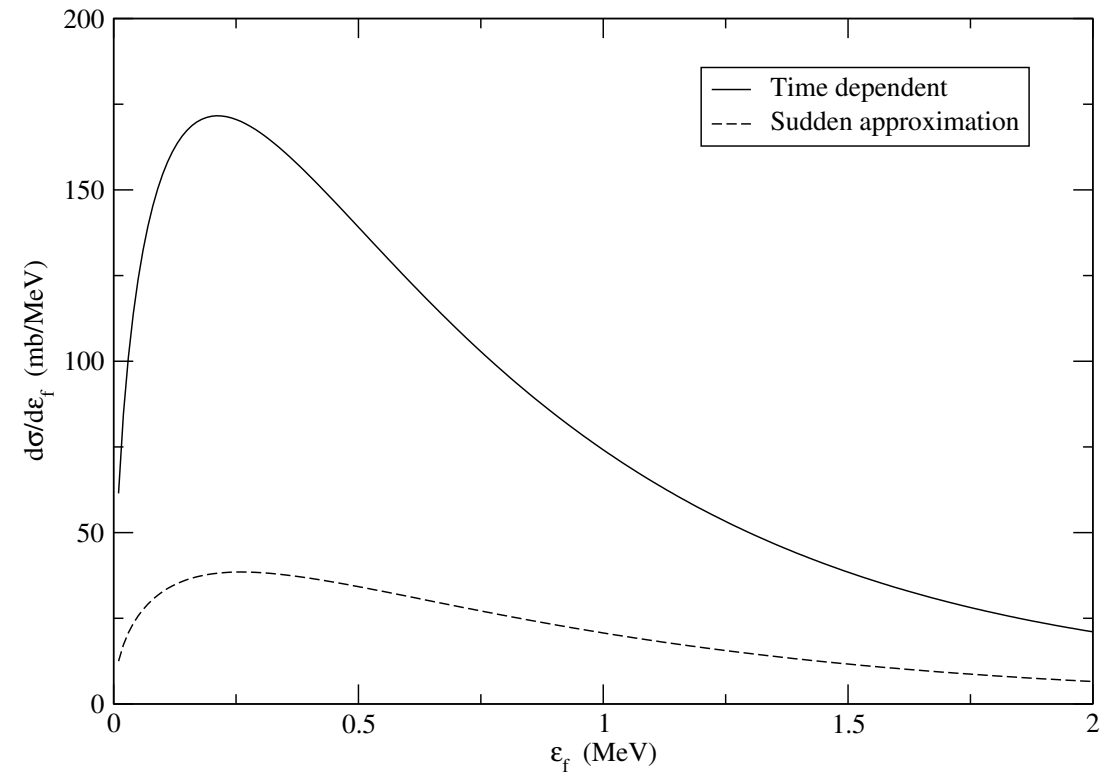
$\delta V$  = correction which originates from particle-vibration couplings.

*(N. Vinh Mau and J. C. Pacheco, Nucl. Phys. A607 (1996) 163.)*

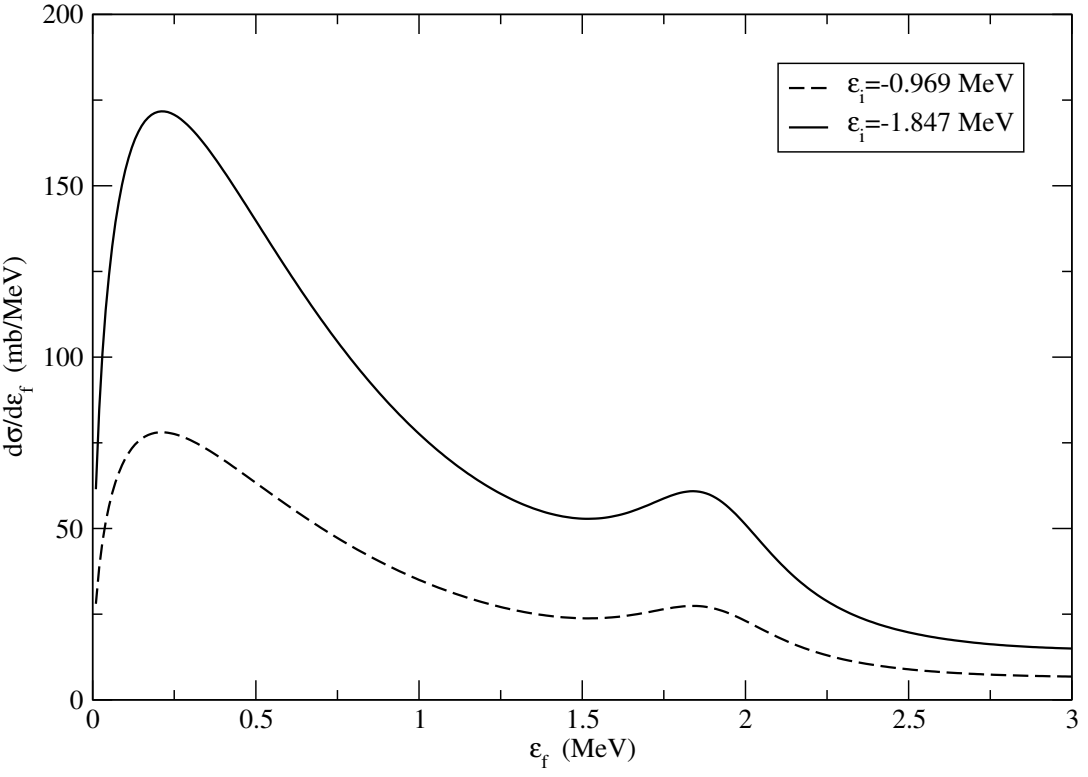
# Potential correction.



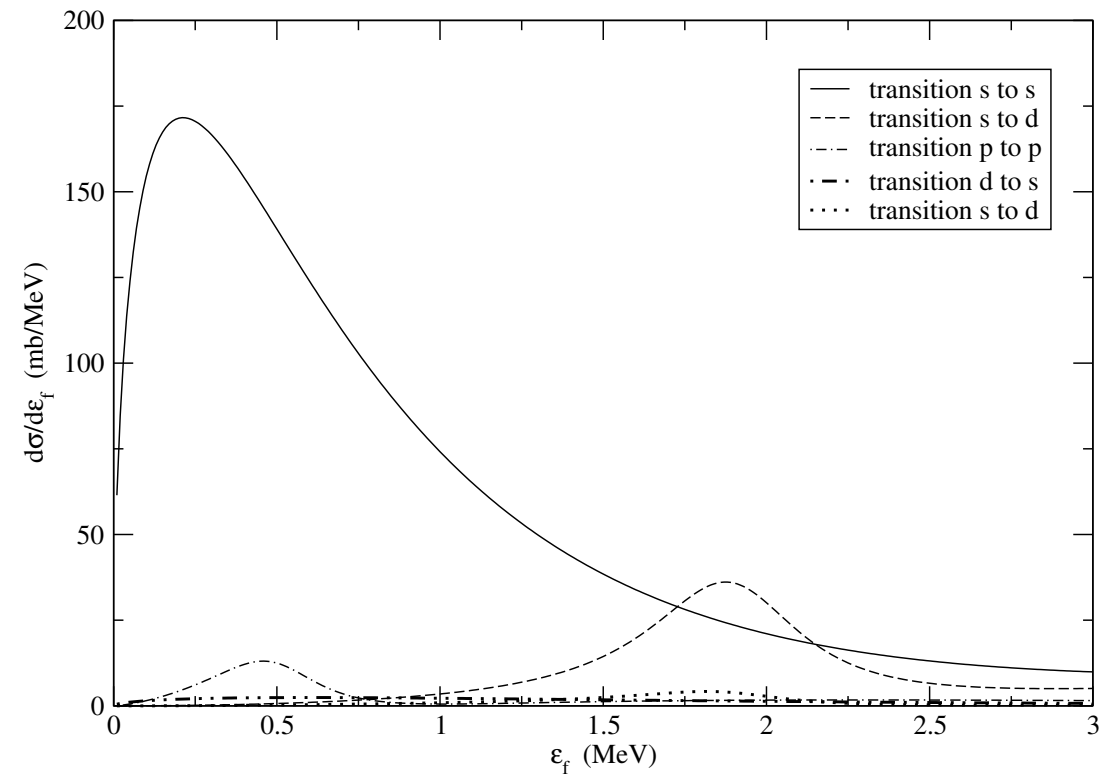
# Comparison between time dependent and sudden approximation.



# Dependence on the binding energy of the initial state.

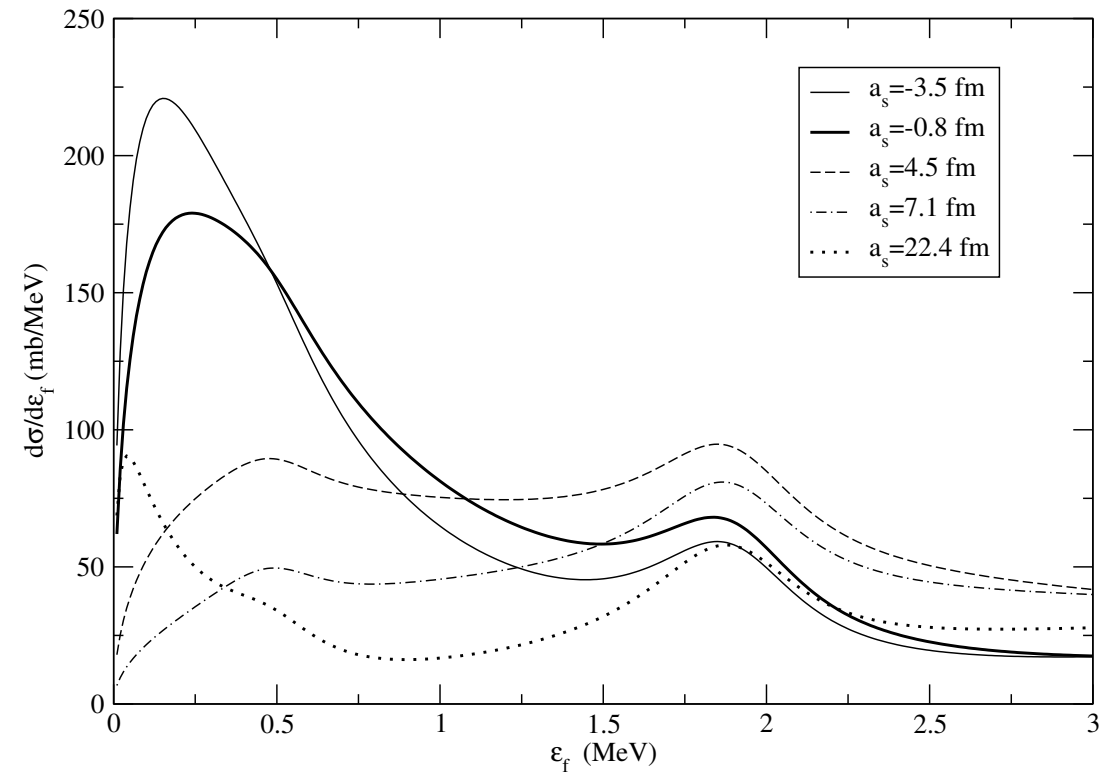


# Strength of every transition.

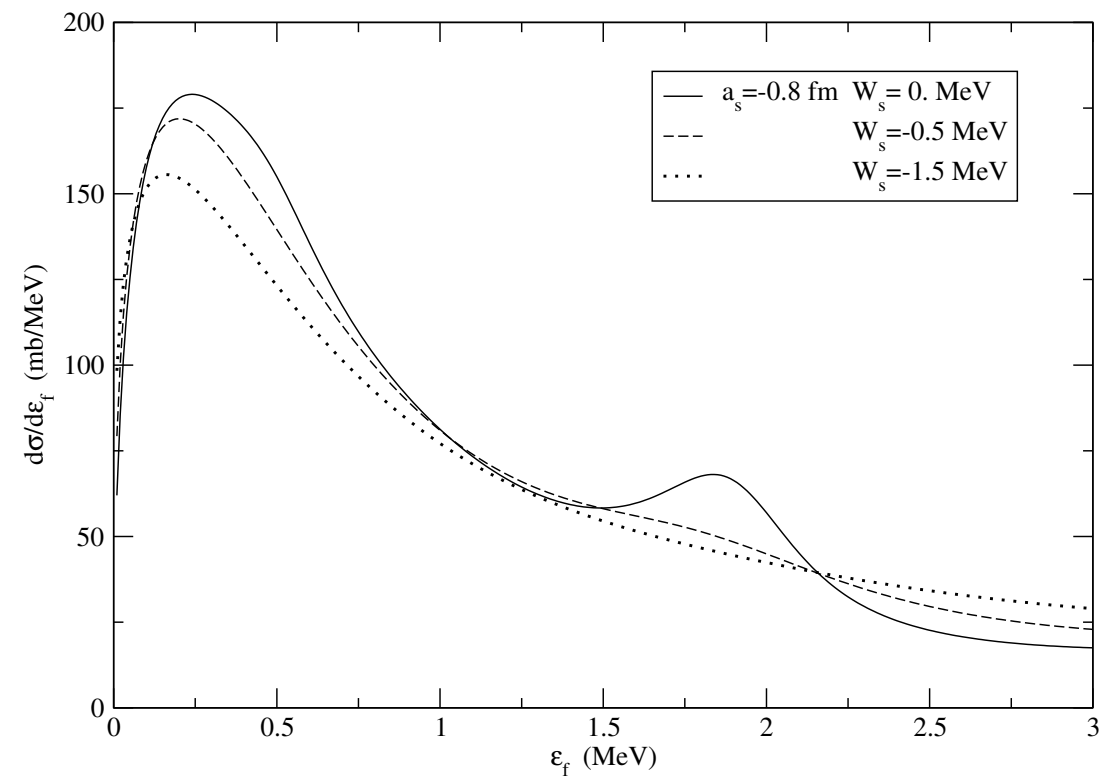




# Dependence on the scattering length of the final s-state.



# Add of a complex part to the potential.



## Conclusions and outlooks

- $^{13}\text{Be}$  is a signature of the halo state of the neutron.
- Possibility to use s resonances.
- One or two steps calculation.