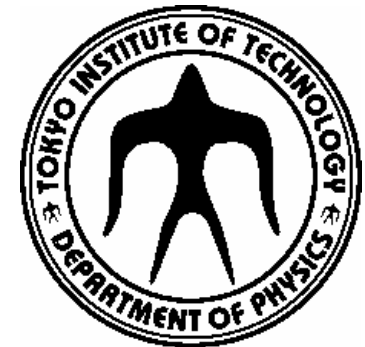


Invariant Mass Spectroscopy and Exotic Structures of Halo Nuclei

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Tokyo Institute of Technology



Unbound Nuclei Workshop
Pisa, Italy 3-5 Nov. 2008

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Inelastic scattering of $^{19,17}\text{C}$ on proton target

Y.Satou, TN et al., Phys. Lett. B660, 320 (2008).

2

Coulomb Breakup of ^{11}Li

T. Nakamura, A.M.Vinodkumar et al., Phys. Rev. Lett. 96, 252502 (2006).

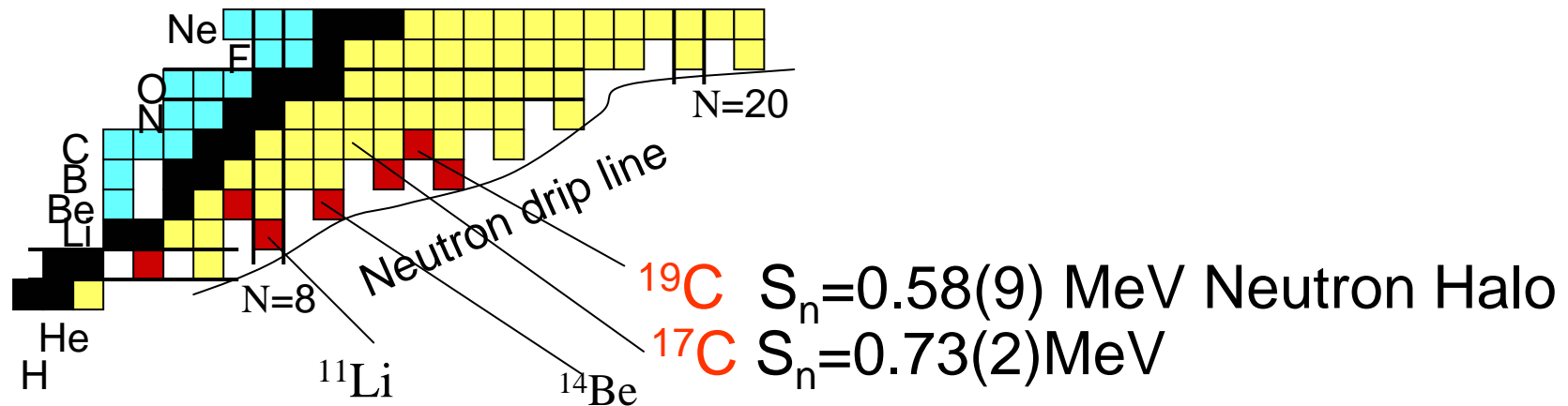
3

SAMURAI/NEBULA Project at RIKEN RIBF

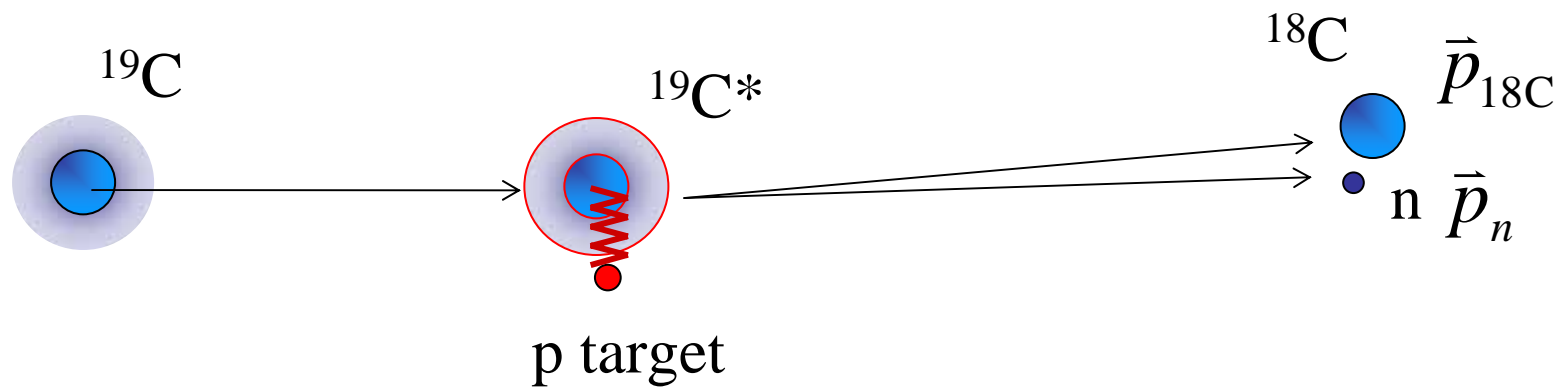
1 Inelastic scattering of $^{19,17}\text{C}$ on proton target

Y.Satou, TN et al.,

Phys. Lett. B 660, 320(2008).



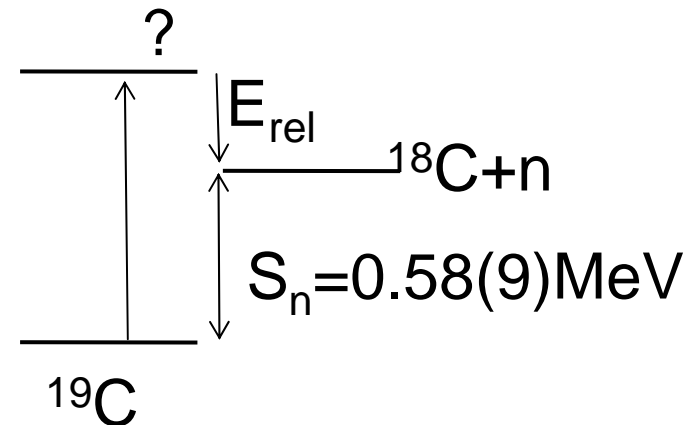
(p,p') inelastic scattering in the inverse kinematics
(Breakup channel)



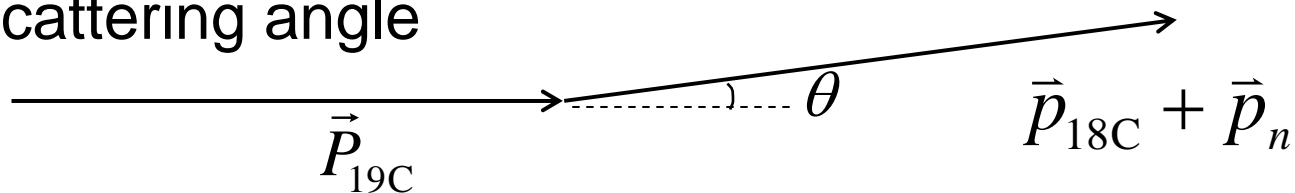
Invariant Mass Method

$$M = \sqrt{(E_{18C} + E_n)^2 - (\vec{P}_{18C} + \vec{P}_n)^2}$$

$$E_{rel} = M - m_{18C} - m_n$$

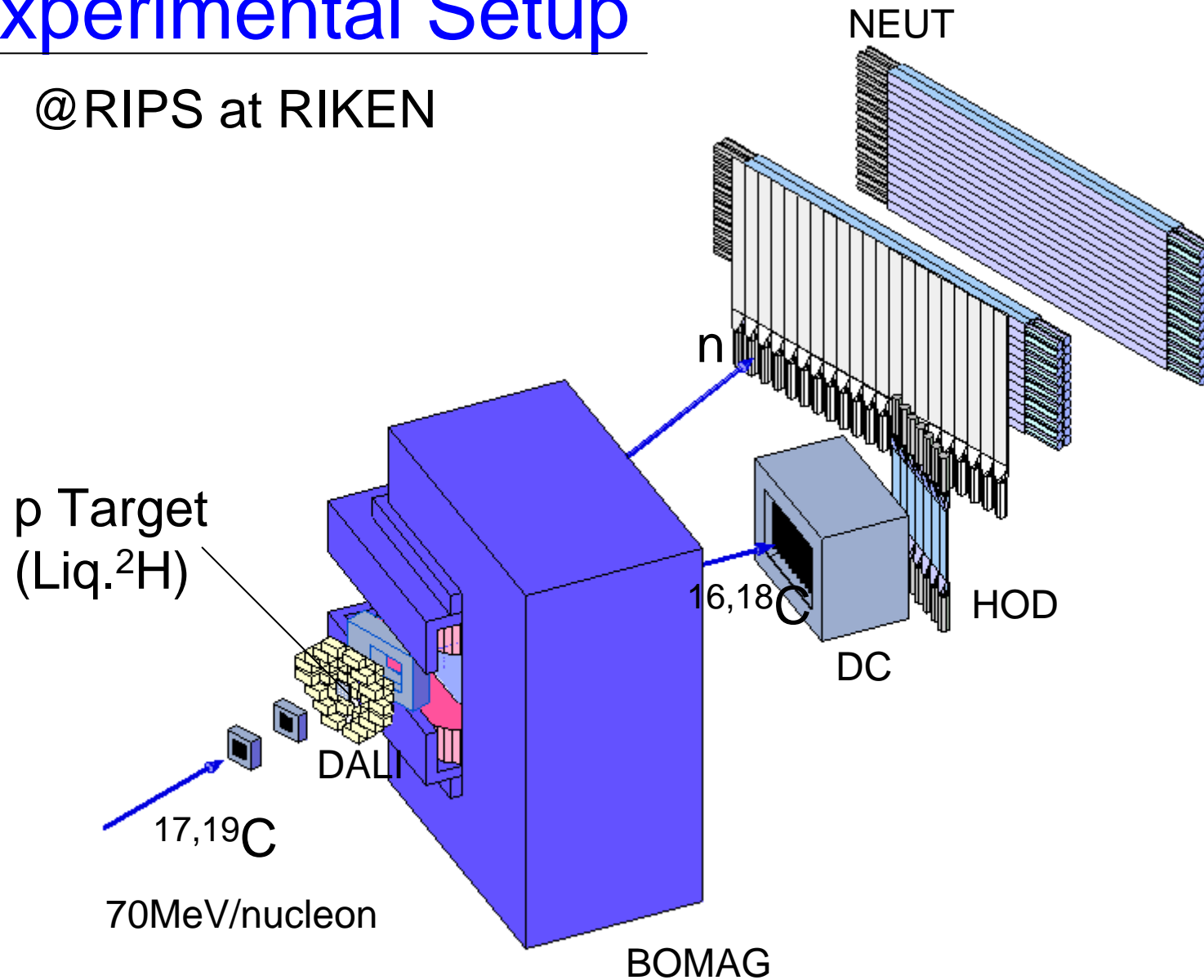


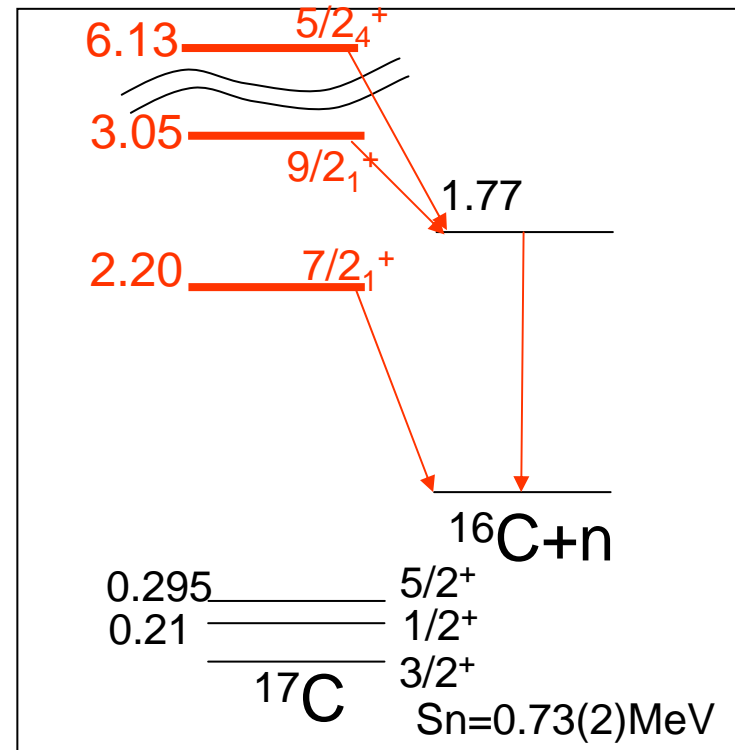
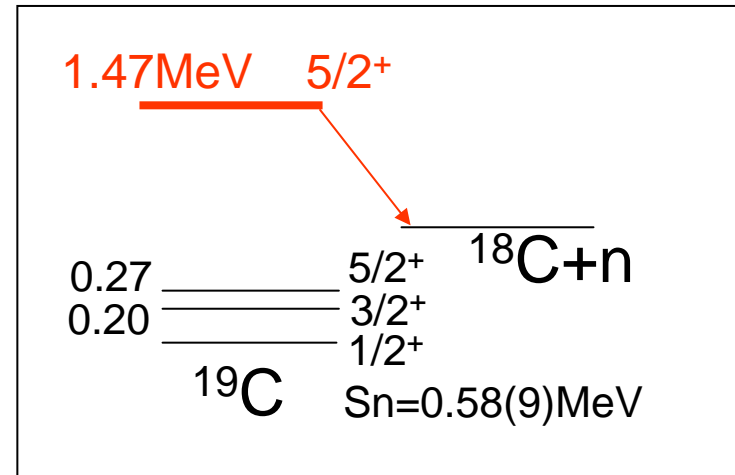
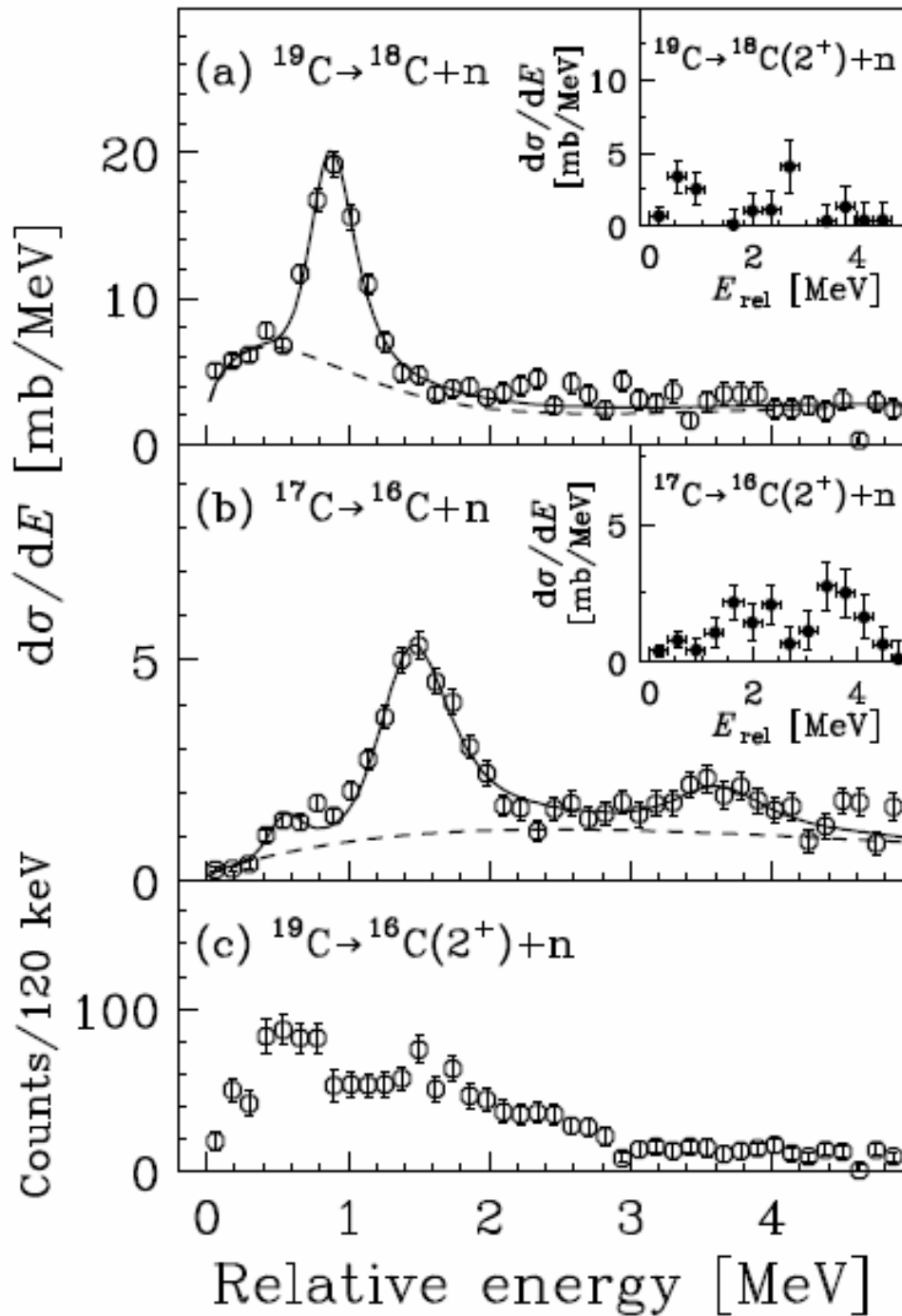
Scattering angle



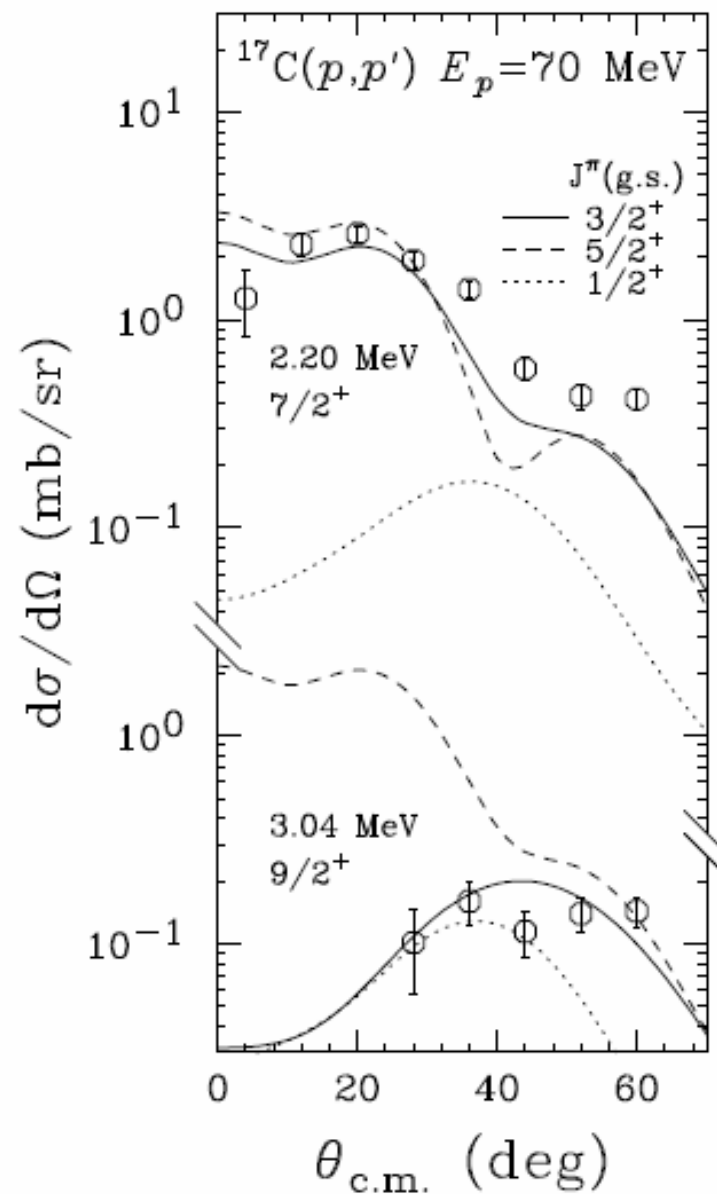
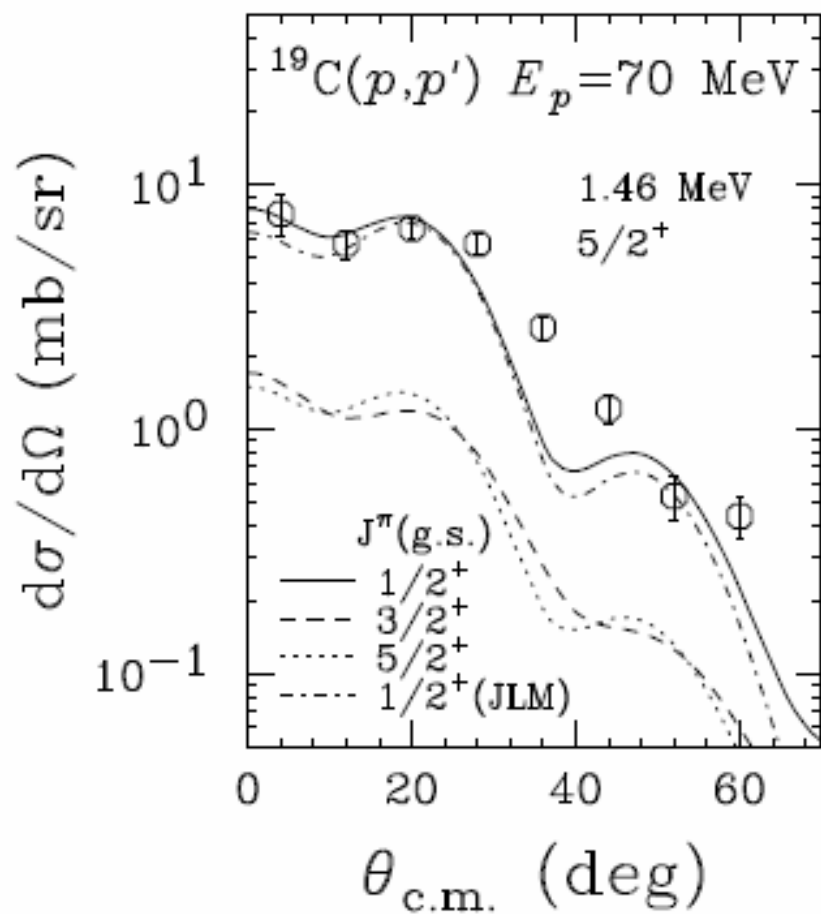
Experimental Setup

@RIPS at RIKEN



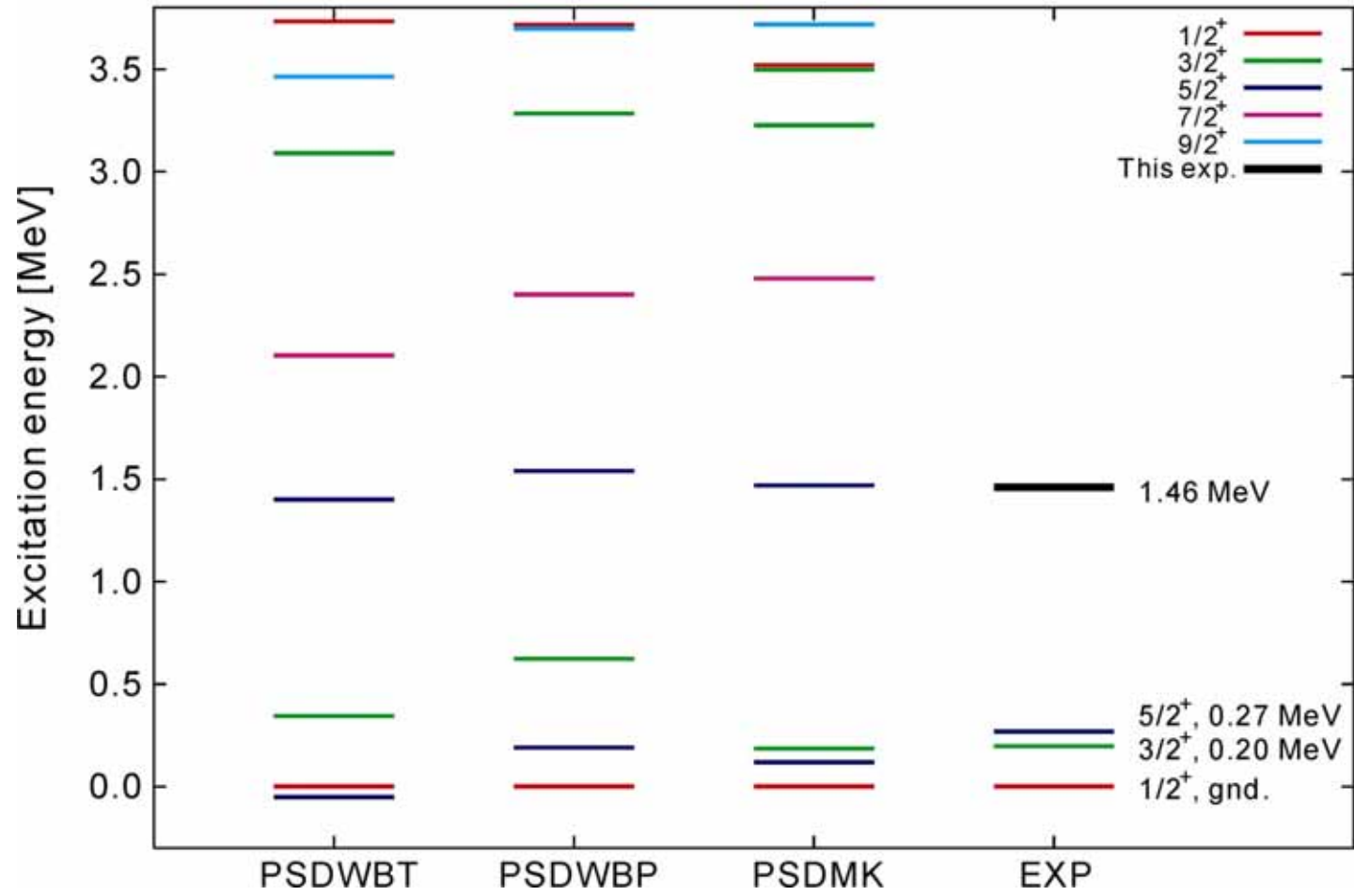


c.f. H.G.Bohlen et al., Eur. Phys. J. A31, 279 (2007).

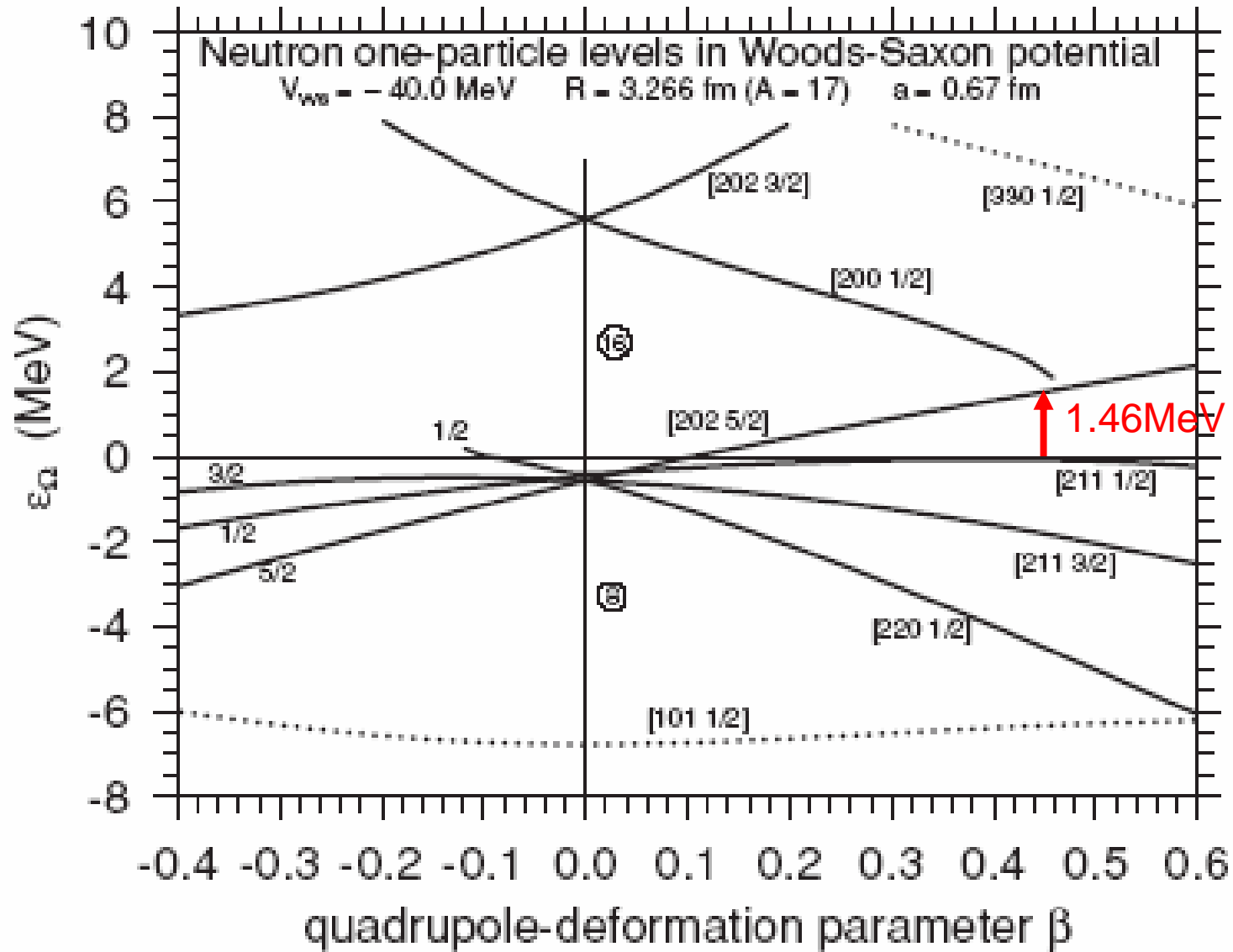


Optical Potential KD02, JLM(dotdash)
 Interaction(projectile-p) M3Y
 Shell model: WBT

Energy level diagram of ^{10}C



$^{19}\text{C } 1/2^+ \rightarrow 5/2_2^+(1.46\text{MeV})$

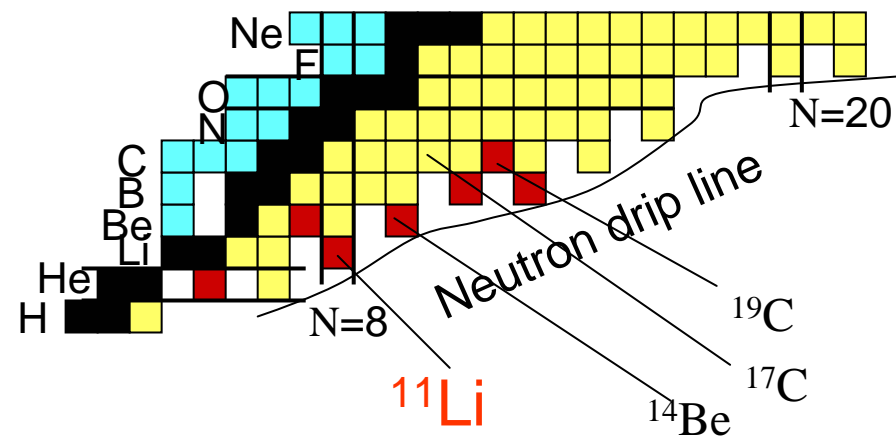


Nilsson diagram is from I. Hamamoto PRC, 2007.

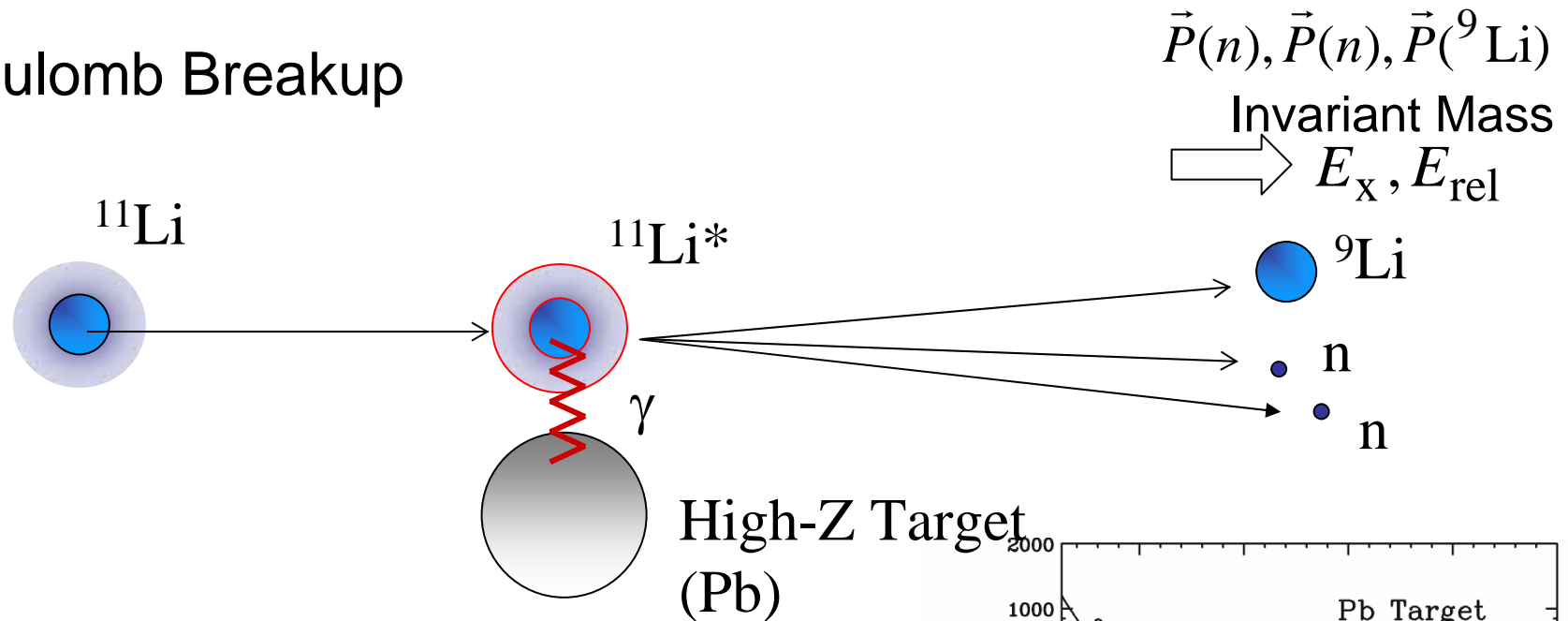
$[211 \ 1/2] \rightarrow [202 \ 5/2]?$

2 Coulomb Breakup of ^{11}Li and two-neutron correlation

T. Nakamura, A.M.Vinodkumar et al.,
Phys. Rev. Lett. 96, 252502 (2006).



Coulomb Breakup

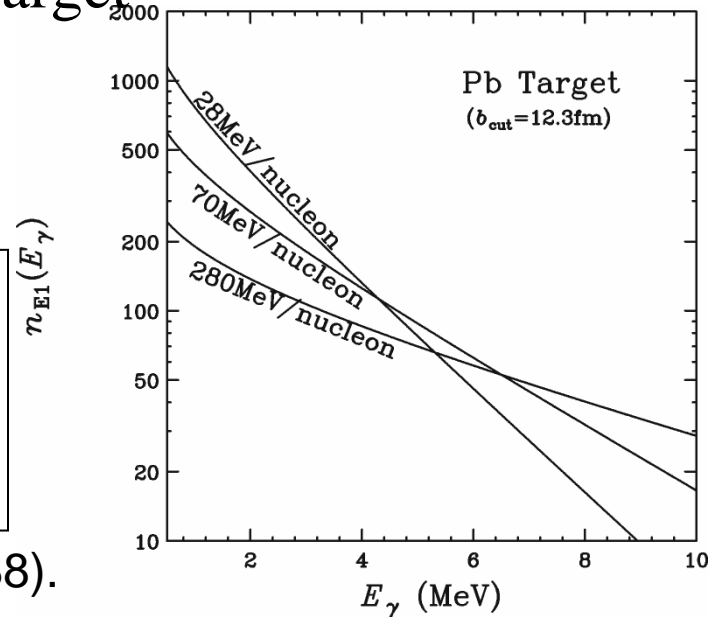


Equivalent Photon Method

$$\frac{d\sigma_C}{dE_x} = \frac{16\pi^3}{9\hbar c} N_{E1}(E_x) \frac{dB(E1)}{dE_x}$$

Cross section = (Photon Number) x (Transition Probability)

e.g. C.A.Bertulani, G.Baur, Phys.Rep.163.299(1988).



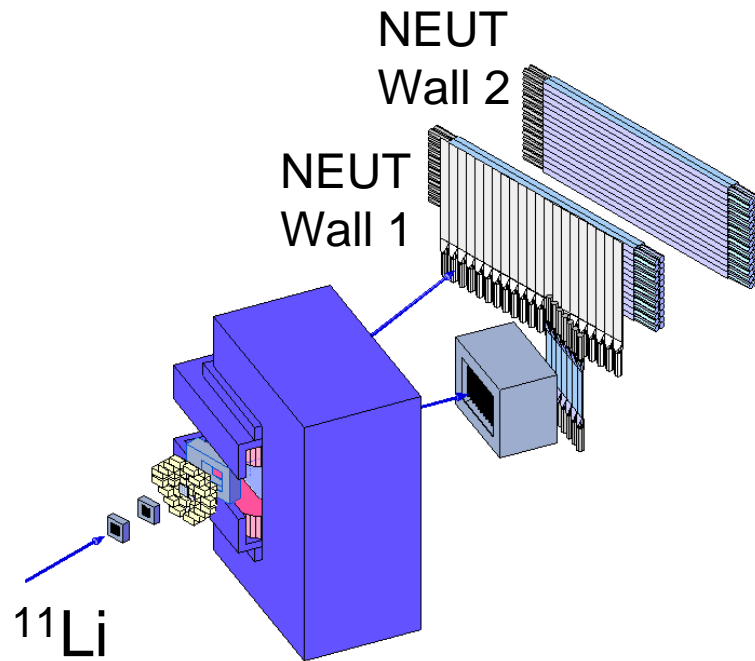
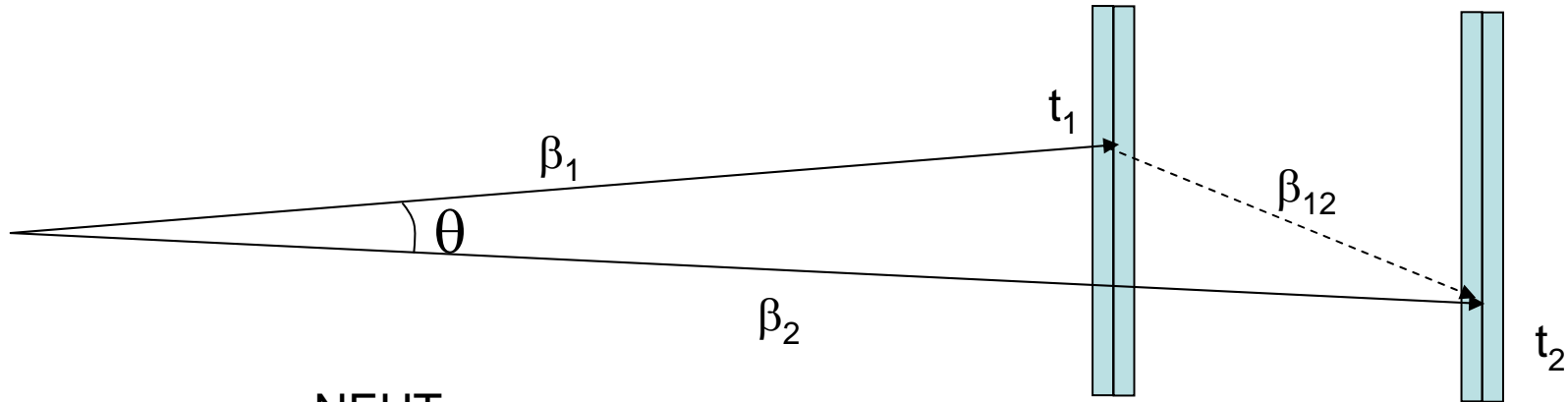
Strong Low-energy E1 transitions (Soft E1 excitation)
 -----Unique property of Halo Nuclei

Elimination of Cross-Talk events

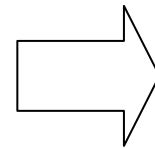
Examine Different Wall Events

Condition: $\beta_1 \leq \beta_{12}$

Almost no bias



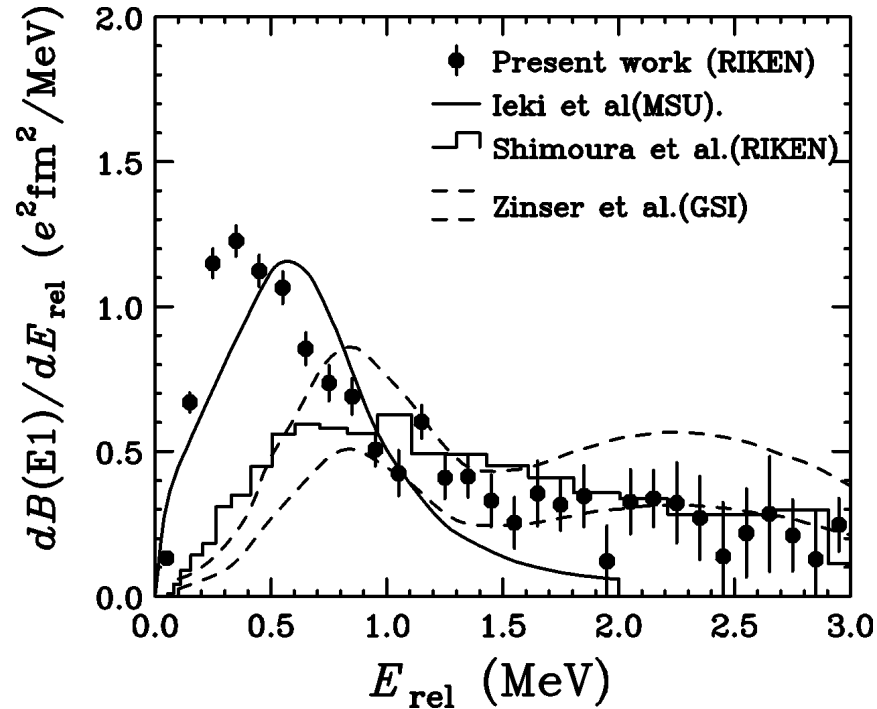
High detection sensitivity
even at $E_{\text{rel}} \sim 0 \text{ MeV}$ ($\theta \sim 0$)



Precise measurement
of B(E1) distribution of ^{11}Li

Experimental Results

TN et al. PRL96,252502(2006).



$$B(E1) = 1.42 \pm 0.18 e^2 fm^2 (E_{rel} \leq 3MeV)$$

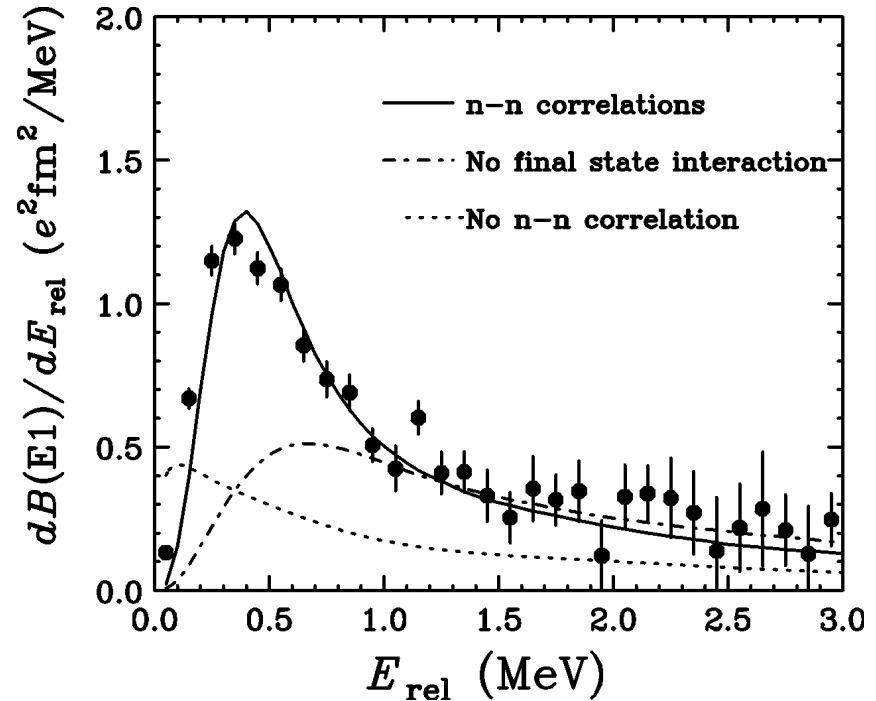
$S_{2n} = 300(19)keV \rightarrow 378(5)keV$

C.Bachelet et al., PRL100,182501(2008).

→ Smaller N(E1)

→ 6% larger B(E1) strength

Comparison with 3-body Theory-1



Calculation

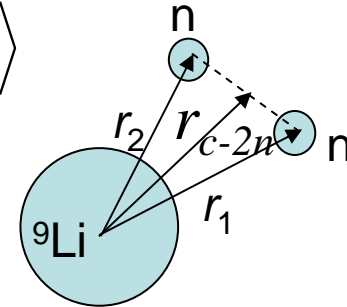
H.Esbensen and G.F. Bertsch
NPA542,310 (1992).

H.Esbensen et al.,
PRC76, 024302 (2007)

Can “Soft E1 of ^{11}Li ” be a signature of “dineutron”?
 Can one determine “Borromean Halo Geometry” from
 “Soft E1” ?

$$B(E1) = \int_{-\infty}^{\infty} \frac{dB(E1)}{dE_x} dE_x = \frac{3}{4\pi} \left(\frac{Ze}{A} \right)^2 \left\langle r_1^2 + r_2^2 + \underline{2(\vec{r}_1 \cdot \vec{r}_2)} \right\rangle$$

$$= \frac{3}{\pi} \left(\frac{Ze}{A} \right)^2 \left\langle \underline{r_{c-2n}^2} \right\rangle$$



$\langle r_{c-2n} \rangle$: directly from B(E1)

$\langle r_1 \cdot r_2 \rangle$: $\langle r_{c-2n} \rangle$ & Non-correlated B(E1) value
 i.e. B(E1) value for $\langle r_1 \cdot r_2 \rangle = 0$

Theoretical. H.Esbensen and G.F. Bertsch, NPA542,310 (1992).

$$B(E1) = 1.42 \pm 0.18 e^2 \text{fm}^2 (E_{\text{rel}} \leq 3\text{MeV})$$

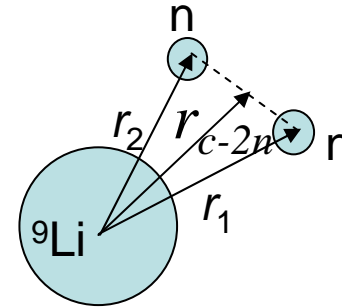
$$\rightarrow 1.78(22) e^2 \text{fm}^2$$

$$\rightarrow \sqrt{\langle r_{c-2n} \rangle^2} = 5.01 \pm 0.32 \text{ fm}$$

~70% larger than non-correlated
 strength $(\vec{r}_1 \cdot \vec{r}_2 = 0)$

$$\longrightarrow \langle \theta_{12} \rangle = 48_{-18}^{+14} \text{ deg}$$

^{11}Li Borromean Geometry



- H.Esbensen et al.,
PRC76, 024302 (2007)

B(E1) or Charge Radius $\rightarrow r_{c-2n}$
 $\langle r_{c-2n} \rangle$ from charge radius is larger by 10-20%
 \rightarrow Core excitation?

- C.A. Bertulani and M.S.Hussein
PRC76, 051602(R) (2007).

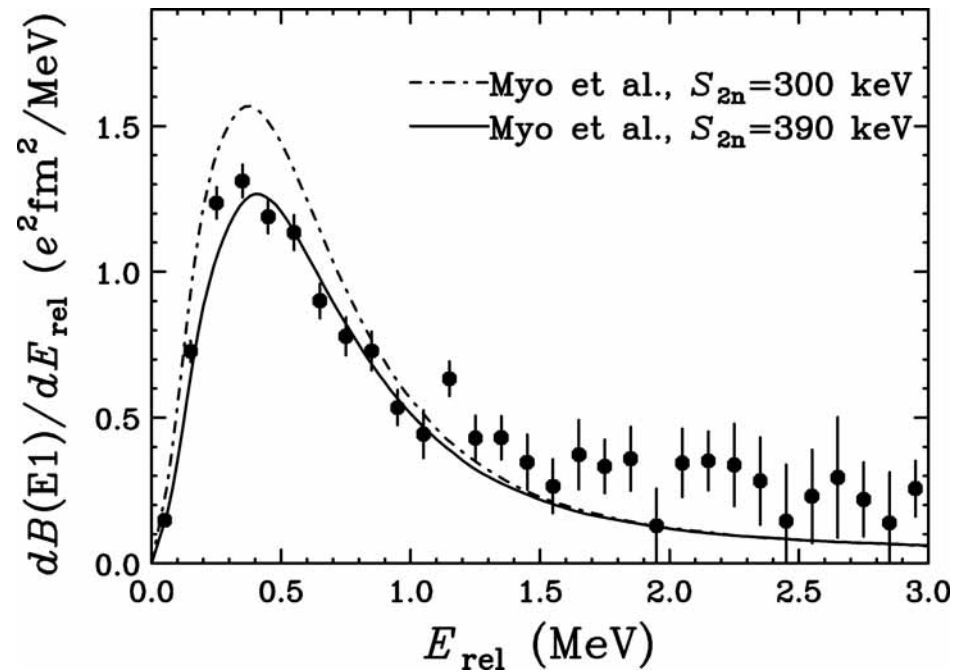
B(E1) or Charge Radius $\rightarrow r_{c-2n}$

Correlation function $\rightarrow r_{nn}$

$$C(\mathbf{p}_1, \mathbf{p}_2) = \frac{P_2(\mathbf{p}_1, \mathbf{p}_2)}{P_1(\mathbf{p}_1)P_1(\mathbf{p}_2)}, \quad r_{nn} \text{ of continuum, not g.s.}$$

Marques et al., PRC64, 061301(R) (2001).

Comparison with 3-body theory-2



Myo et al., PRC76,024305 (2007).

Core polarization

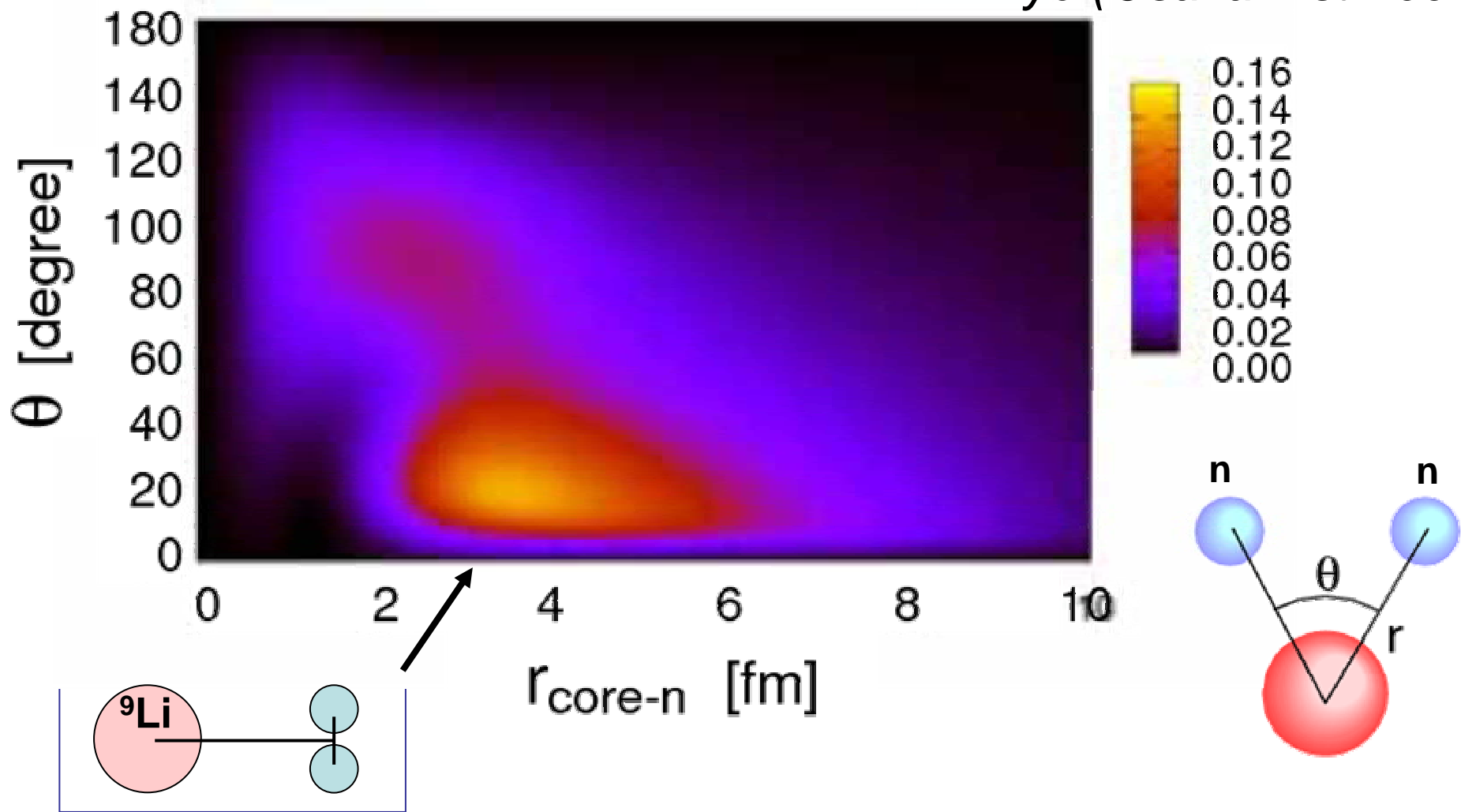
(Tensor correlation+Pauli Principle)

$$P(S^2) \sim 40\% \quad \sqrt{\langle r_{c-2n} \rangle^2} = 5.38 \text{ fm} \quad \langle \theta_{12} \rangle = 65 \text{ deg}$$

Both Charge distribution & B(E1) are reproduced.

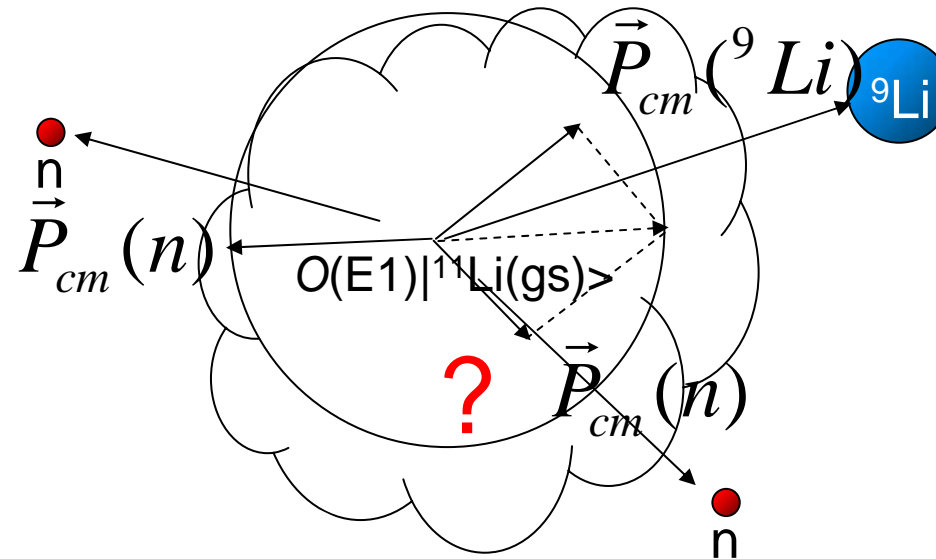
2n correlation density in ^{11}Li

2n density in ^{11}Li Courtesy of
T.Myo (Osaka Inst.Tech)



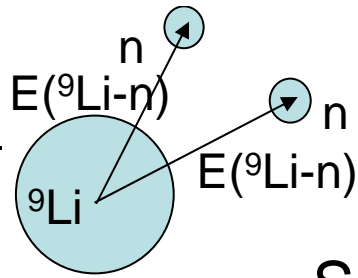
Cf. H.Esbensen and G.F.Bertsch, NPA542(1992)310

2n Correlations can be studied by 3-body decay of $^{11}\text{Li}^*$?

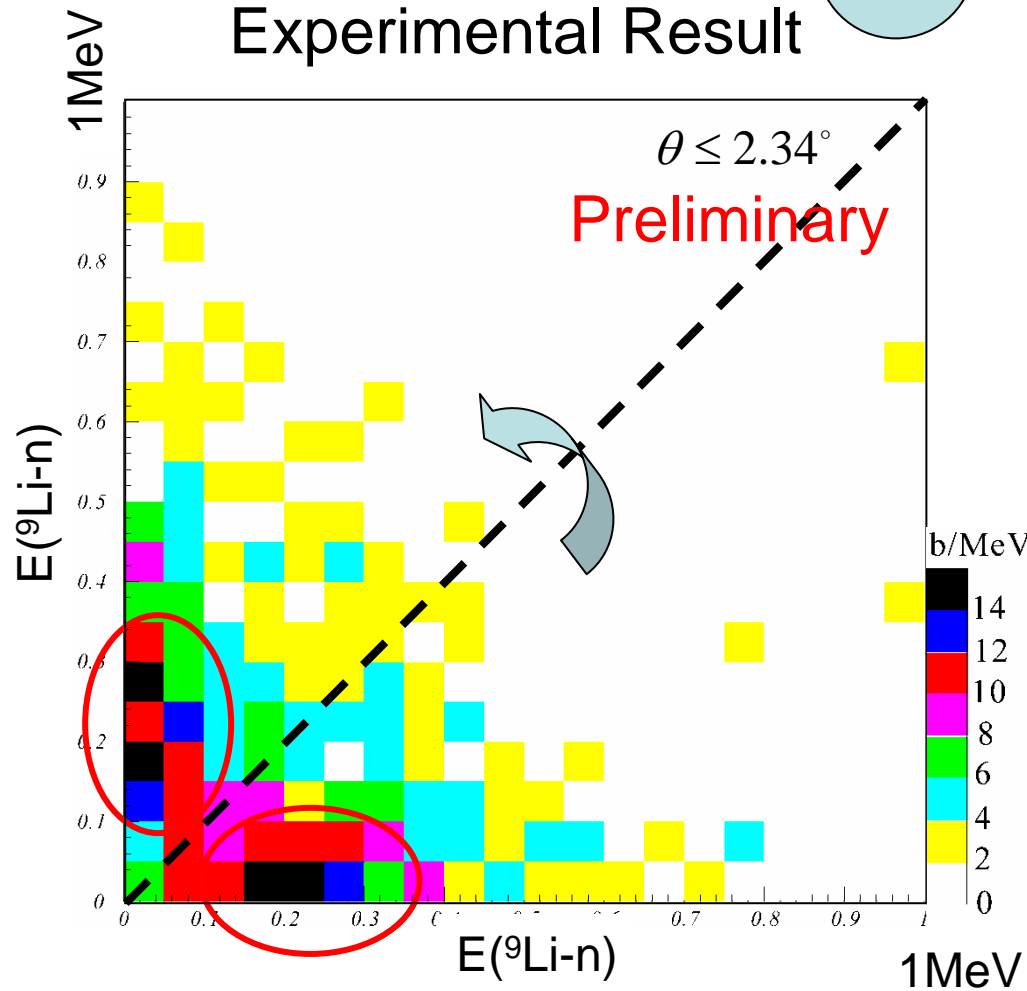


--Kinematically complete measurement

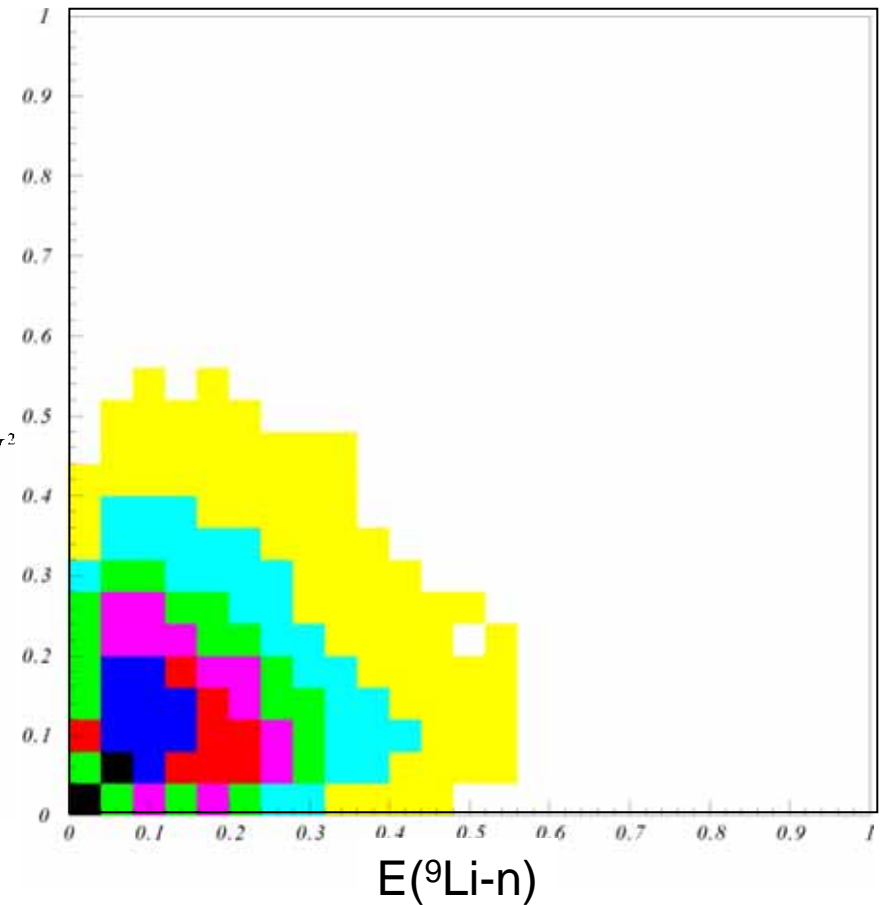
Further Correlation?

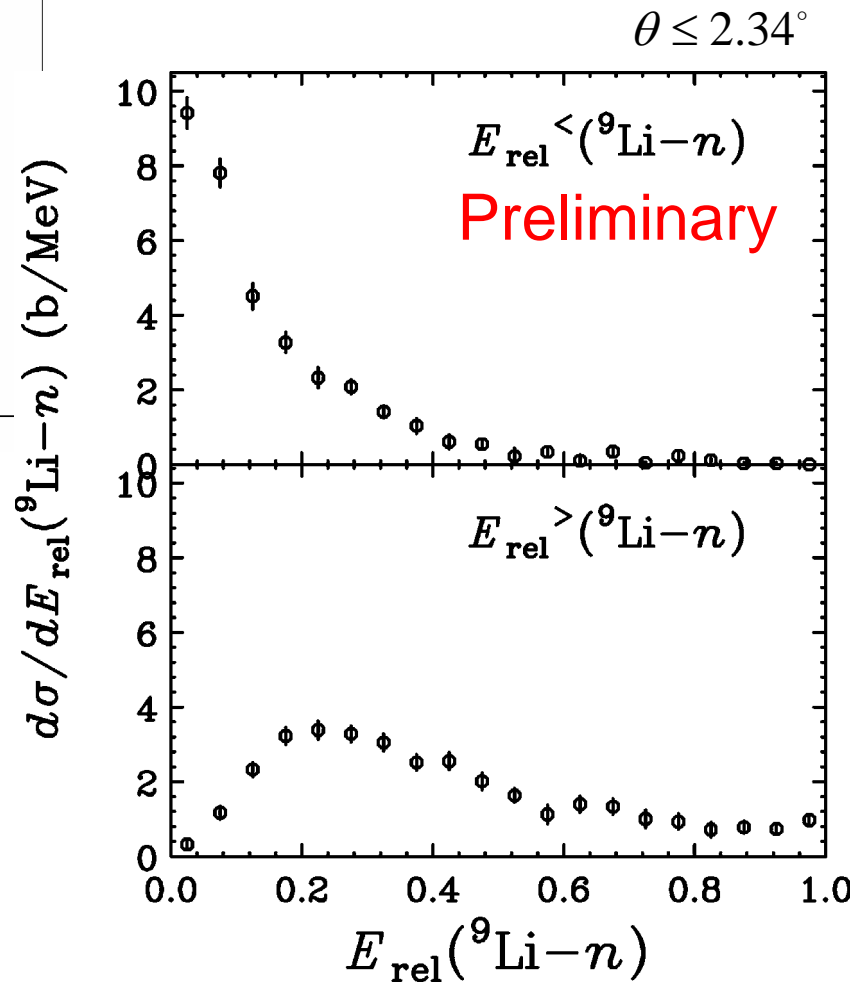
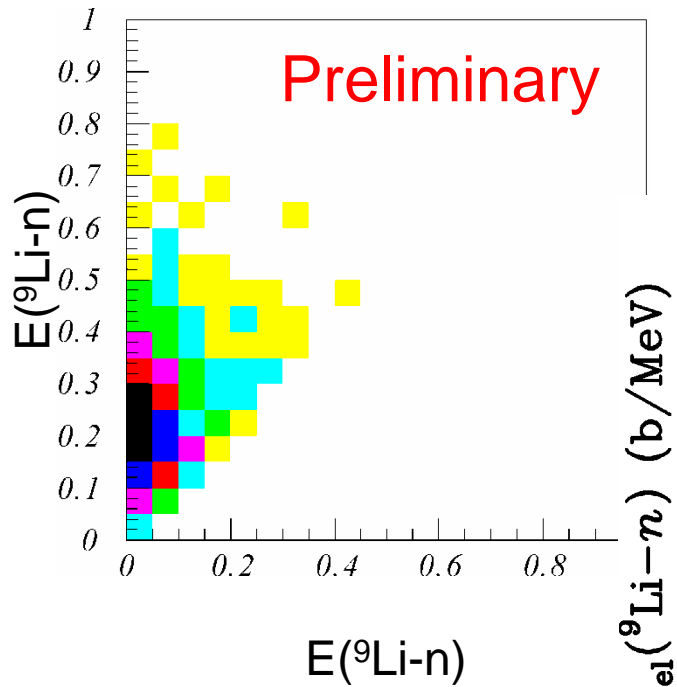


Experimental Result



Simulation (Phase Space)





$$|\Phi(^{11}\text{Li}_{\text{gs}})\rangle = \alpha |\Phi(^9\text{Li}_{\text{gs}}) \otimes (s_{1/2})^2\rangle + \beta |\Phi(^9\text{Li}_{\text{gs}}) \otimes (p_{1/2})^2\rangle + \dots$$

$$|O(E1) | \Phi(^{11}\text{Li}_{\text{gs}})\rangle = \gamma |\Phi(^9\text{Li}_{\text{gs}}) \otimes (s_{1/2})^1 (p_{1/2})^1\rangle + \dots$$

Efimov Effect in Nuclear Three-Body Resonance Decays

E. Garrido

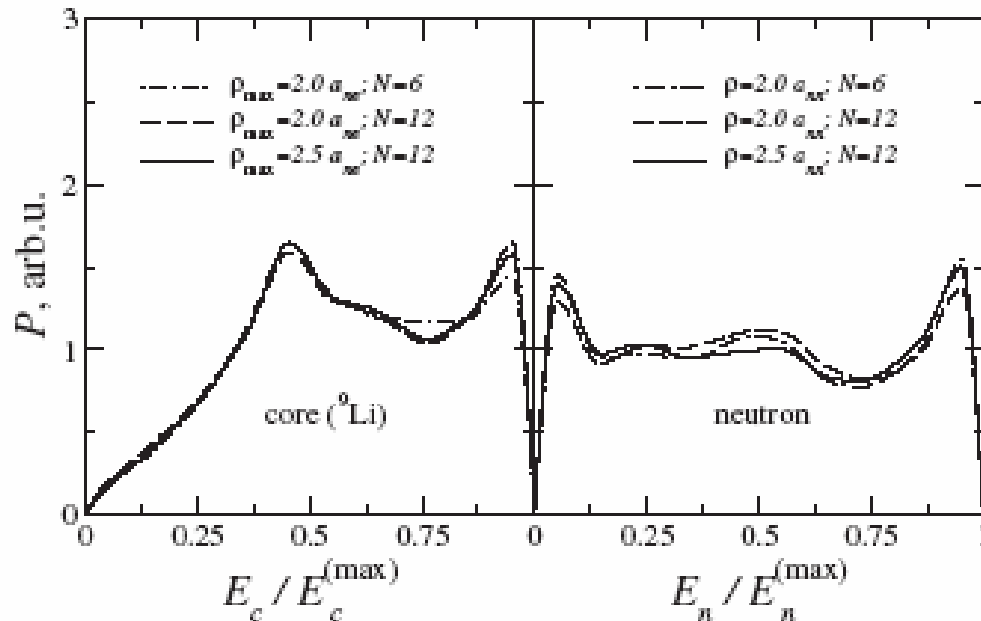
Instituto de Estructura de la Materia, CSIC, Serrano 123, E-28006 Madrid, Spain

D. V. Fedorov and A. S. Jensen

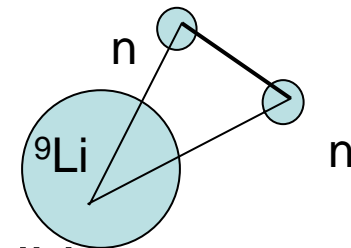
Department of Physics and Astronomy, University of Aarhus, DK-8000 Aarhus C, Denmark

(Received 7 July 2005; published 20 March 2006)

Investigate 1^- state in ^{11}Li



Energy distribution of core (^9Li) and n in the decay of **E1 state of ^{11}Li**

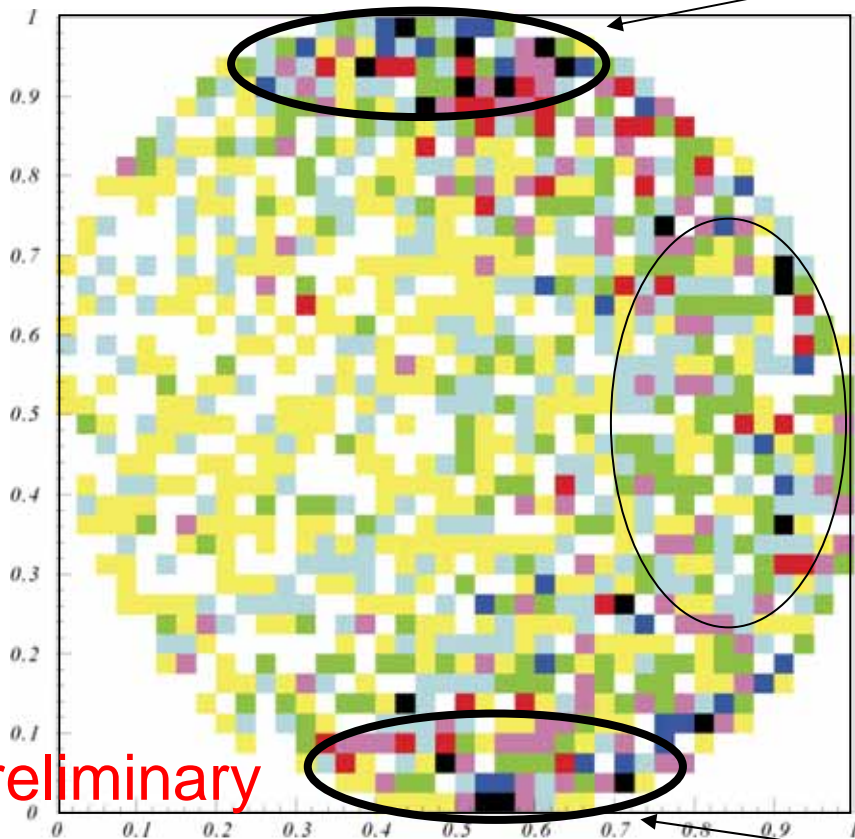


Efimov Condition:

At least 2-out-of-3 two-body scattering lengths are large

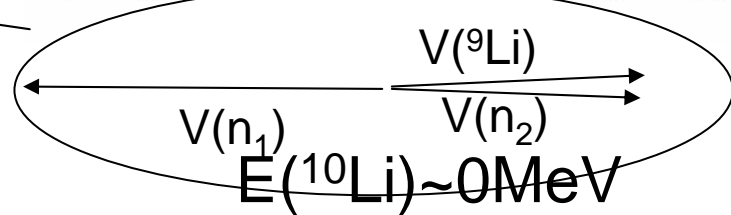
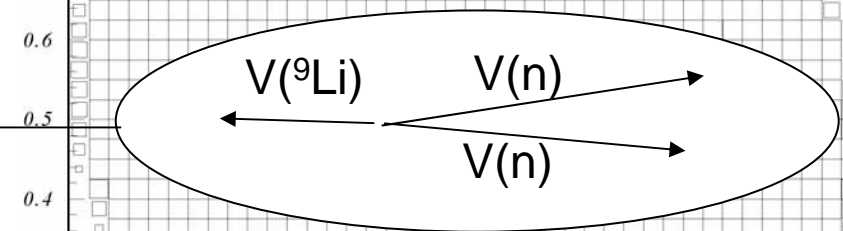
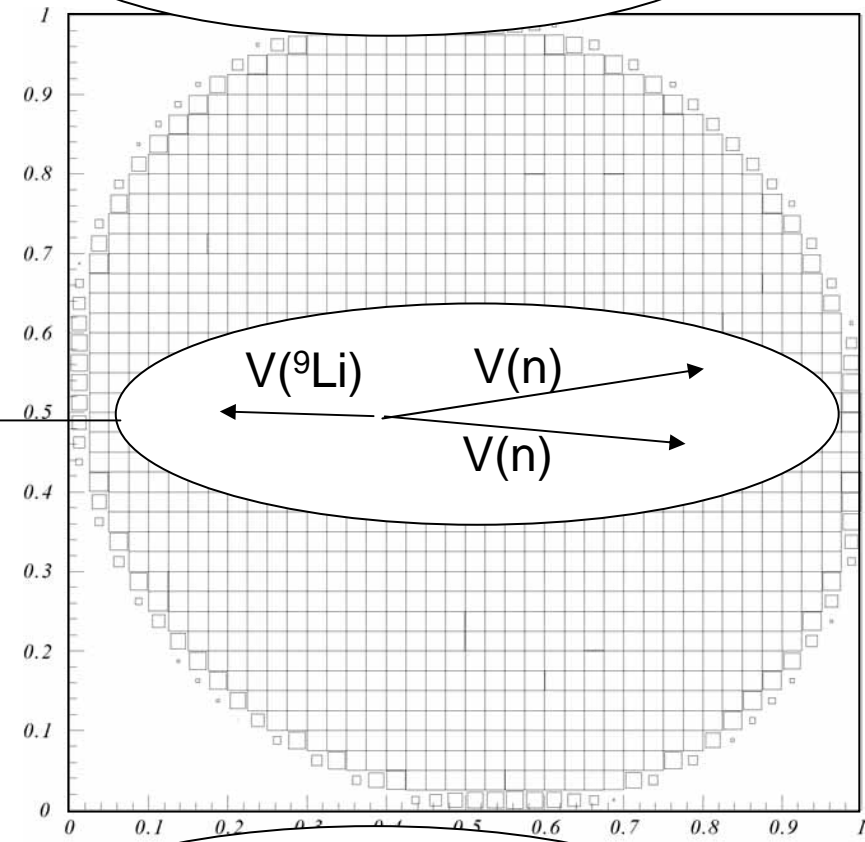
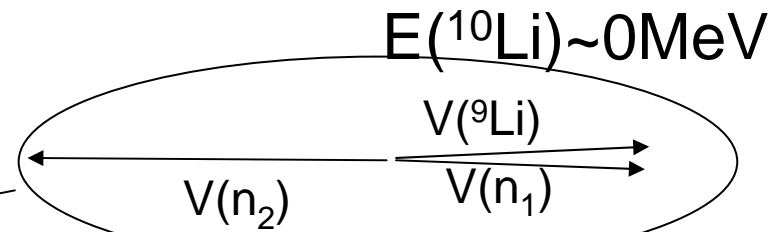
$$a(^9\text{Li}n) \sim a(nn) \sim 20 \text{ fm}$$

$$\frac{E_{rel}(3body) - E_{rel}({}^9Li, n)}{E_{rel}(3body)} = \frac{E_n}{E_n^{(max)}} \quad \text{Experiment}$$



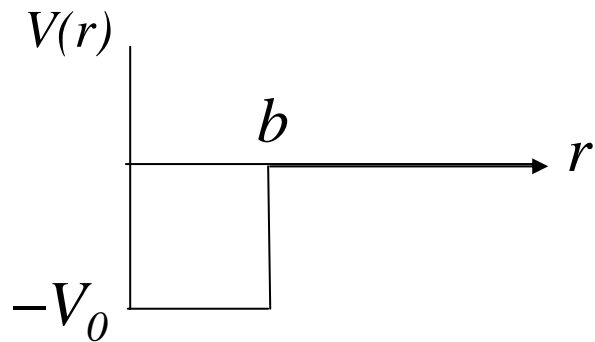
Preliminary

$$\frac{E_{rel}(3body) - E_{rel}(nn)}{E_{rel}(3body)} = \frac{E_c}{E_c^{(max)}}$$



memo Scattering length

$V(r)$ —Potential between n and A
 (A can be ${}^9\text{Li}$ or n or whatever)

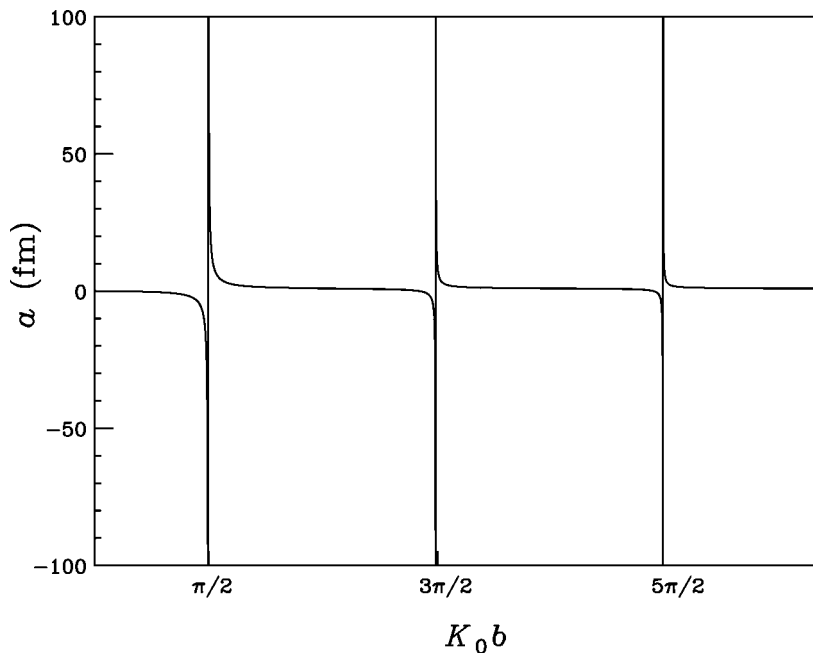


For a square well potential,

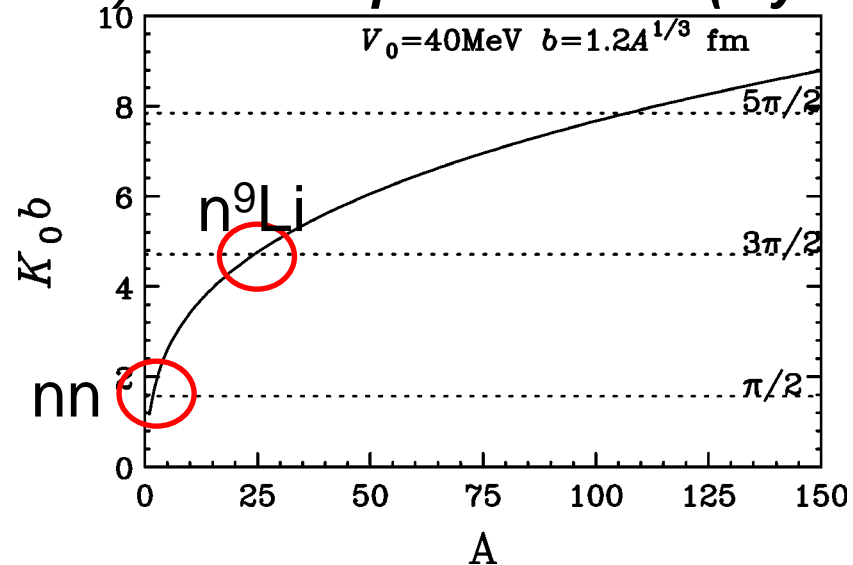
$$a = b \left[1 - \frac{\tan K_0 b}{K_0 b} \right], \quad K_0 = \frac{\sqrt{2\mu V_0}}{\hbar}$$

$$\lim_{k \rightarrow 0} \sigma = 4\pi a^2, \quad k \cot \delta = -\frac{1}{a} + \frac{1}{2} k^2 r_0$$

a can be “negatively very large” only when
 there is **an unbound state** under a **specific potential condition**



$V(n-{}^9\text{Li})$ is as deep as $\sim 65\text{MeV}$ (Myo et al.,

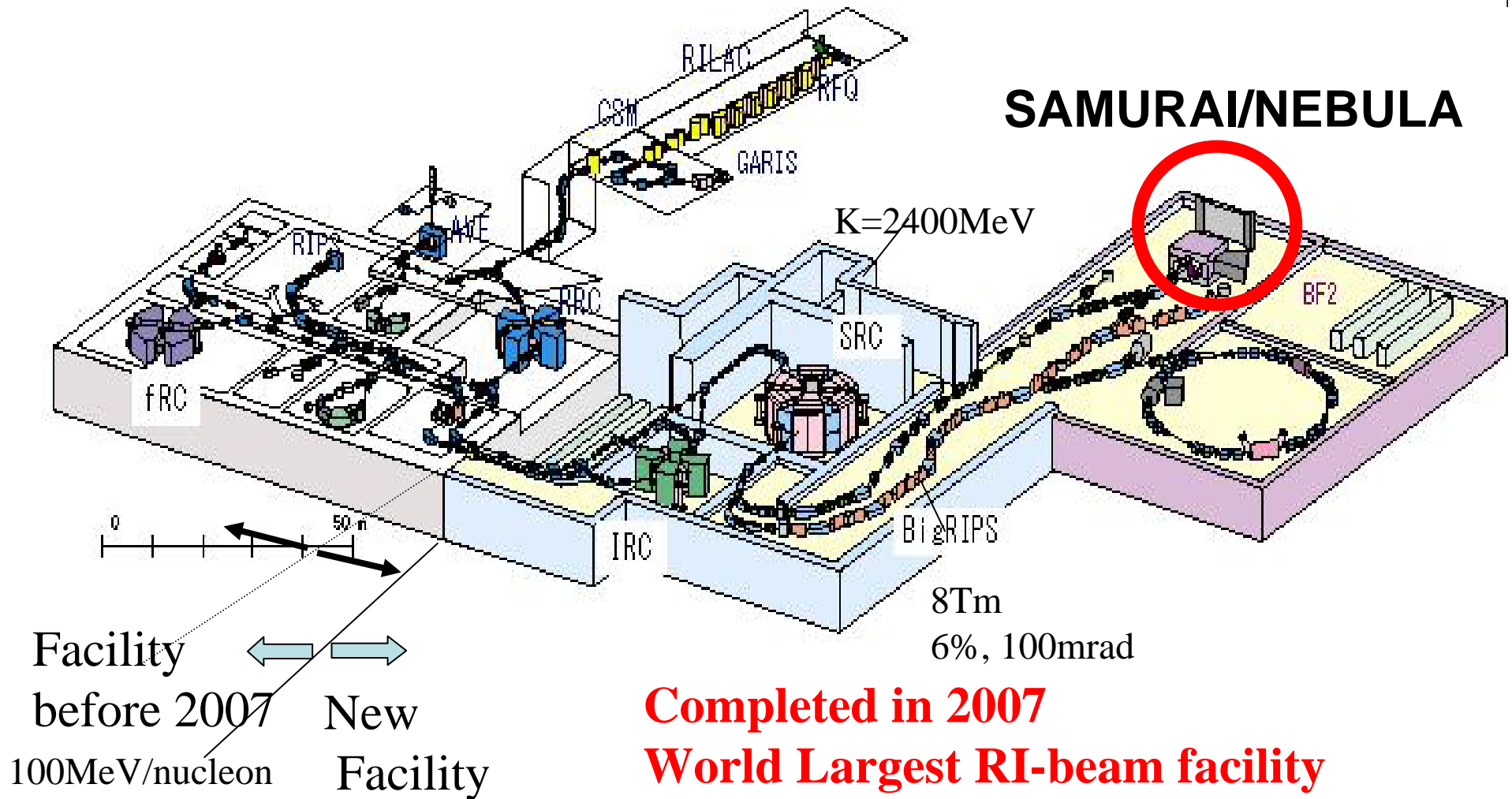


$$a(nn) = -18.5\text{fm}, \quad a({}^9\text{Li}, n) = -10 \sim -25\text{fm}$$

3

SAMURAI / NEBULA PROJECT @ RIKEN RI BEAM FACTORY

RIBF (RIKEN RI Beam Factory)



350MeV/nucleon, ~1pμA
Heavy ions up to U beam

SAMURAI

Superconducting **A**nalyser for **M**ulti-particles from **R**adio-Isotope Beam

Funded! 2008-2011 1.5GJPY~15MUSD~12MEuro

(10MEuro 1Month Ago)

Superconducting Magnet

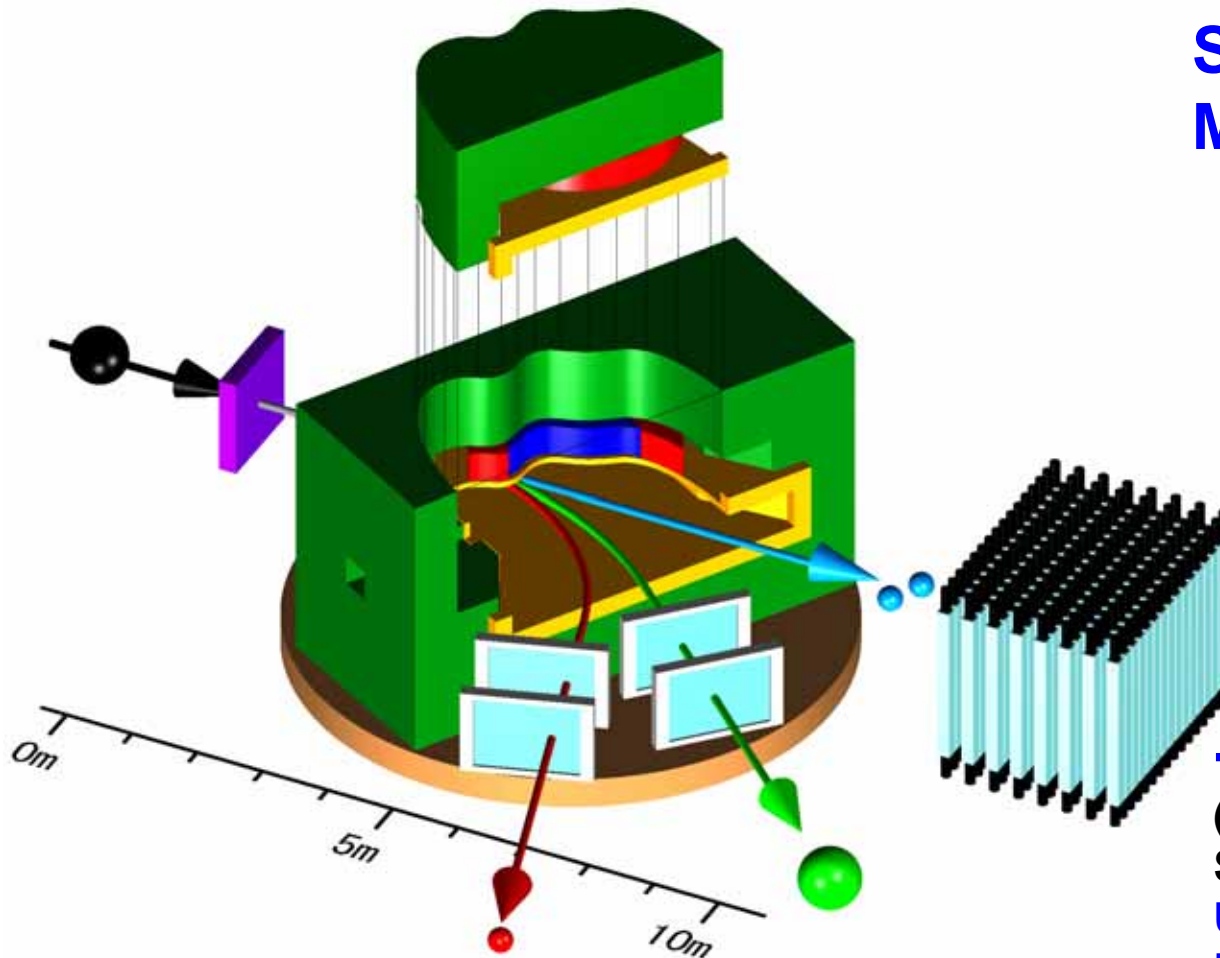
To let neutron(s) pass through the gap

Sweep Beam and Charged Fragments

Good Mass Resolution for PID @ A~100

+NEBULA

(**N**eutron Detection System for **B**reakup of **U**nstable Nuclei with **L**arge **A**cceptance)



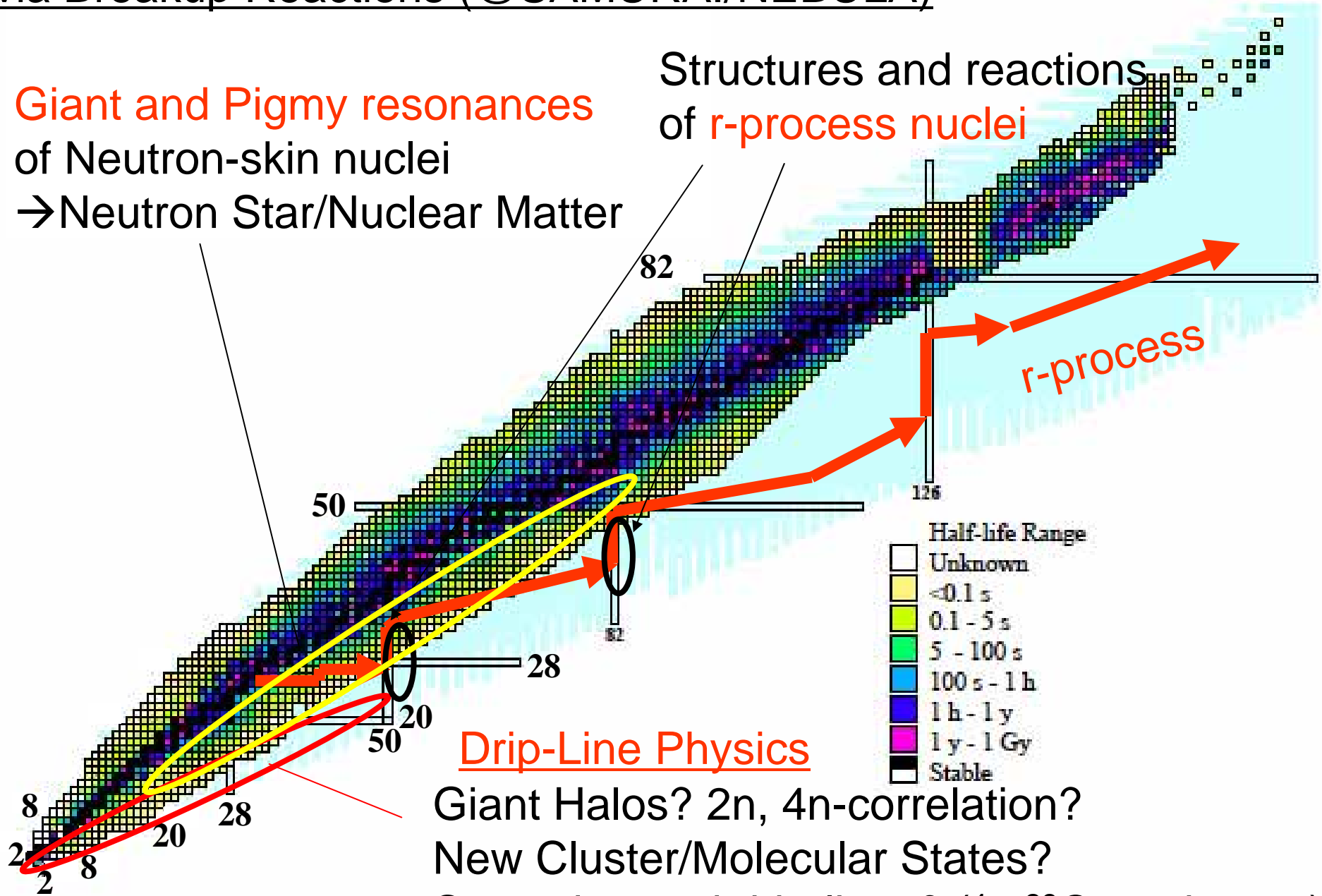
Bending Power

BL=7Tm (B=3Tesla, 60deg bending)

PHYSICS OF NEUTRON-RICH NUCLEI
via Breakup Reactions (@SAMURAI/NEBULA)

Giant and Pigmy resonances
of Neutron-skin nuclei
→ Neutron Star/Nuclear Matter

Structures and reactions
of r-process nuclei



Drip-Line Physics

Giant Halos? $2n$, $4n$ -correlation?
New Cluster/Molecular States?
States beyond drip-lines? ($4n$, ^{28}O , and more)

Summary

1 Inelastic scattering of $^{19,17}\text{C}$ on proton target

Y.Satou, TN et al., Phys. Lett. B 96, 252502 (2008).

- (p,p') with DWBA: useful tool
- ^{19}C : $1/2^+ \rightarrow 5/2_2^+$ at 1.47MeV (new state) ; ^{17}C : 3 transitions

2 Coulomb Breakup of ^{11}Li and two-neutron correlation

T. Nakamura, A.M.Vinodkumar et al., Phys. Rev. Lett. 96, 252502 (2006).

- Strong B(E1) at very low excitation energy $B(E1) = 1.42 \pm 0.18 e^2 fm^2 (S_{2n} = 300\text{keV})$
 $B(E1) = 1.50 \pm 0.19 e^2 fm^2 (S_{2n} = 378\text{keV})$
- neutron-neutron spatial correlation from E1 sum rule $\theta_{nn} \sim 50\text{-}60\text{deg}$
- 3-body decay of Dipole state of ^{11}Li ----Signature of strong virtual state in ^{10}Li and nn
 \rightarrow Efimov?

3 SAMURAI/NEBULA Project

Collaborators

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T. Motobayashi, T. Nakabayashi, T.Okumura, H. Otsu, H.J.Ong,
T.K. Onishi, A.Saito, H.Sakurai, S. Shimoura, M. Shinohara,
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