

# Spectroscopy of Halo Nuclei by Breakup Reactions

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# Contents

## 1 Coulomb Breakup of 1n-Halo Nucleus and Spectroscopic Factors

$^{11}\text{Be}+\text{Pb}$

T.Nakamura et al., PLB331,296(1994)

N.Fukuda et al., in preparation (2004).

$^{15}\text{C}+\text{Pb}$ ,  $^{19}\text{C}+\text{Pb}$

T.Nakamura et al., in preparation (2004).

T.Nakamura et al. PRL 83, 1112 (1999).

## 2 Nuclear Breakup of 1n-Halo Nucleus

$^{11}\text{Be}+\text{C}$

N.Fukuda et al., in preparation (2004).

## 3 Breakup of 2n Halo Nuclei $^{11}\text{Li}$ , $^{14}\text{Be}$ , $^{17}\text{B}$

A.M.Vinodkumar et al., in preparation (2004).  $^{11}\text{Li}$ ,

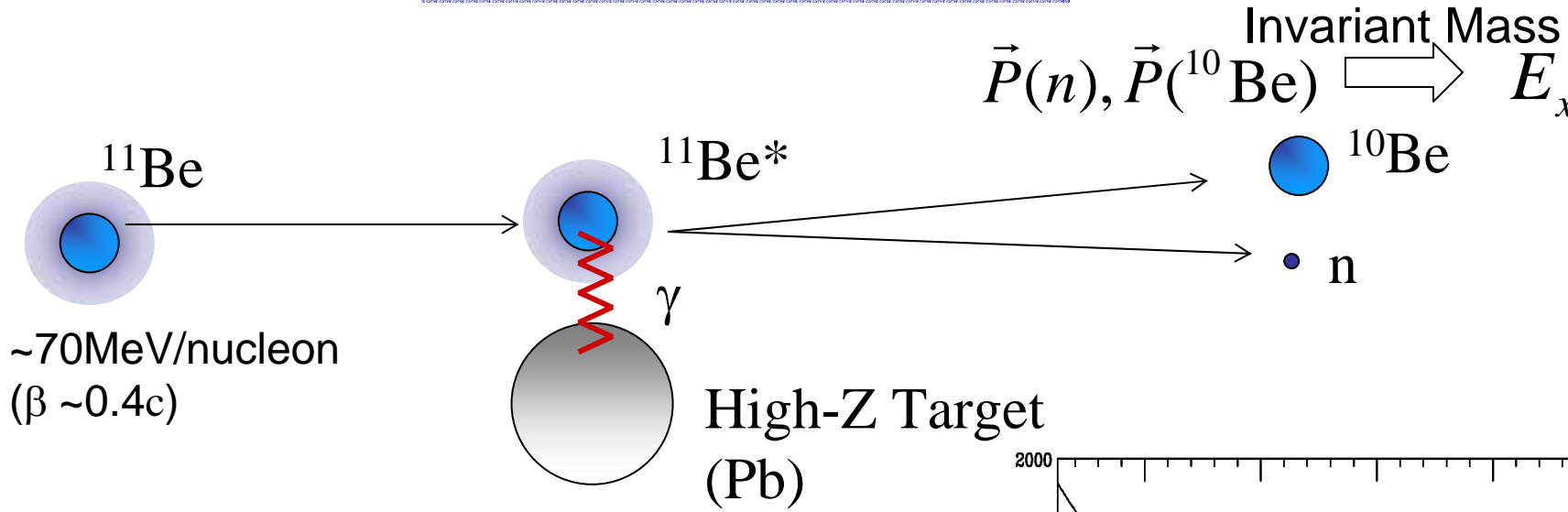
T.Sugimoto, M.Miura et al., in preparation (2004).  $^{14}\text{Be}$

T.Sugimoto et al., in preparation (2004).  $^{17}\text{B}$

Angular Distribution  
+  
 $E_{\text{rel}}$  Spectrum

# Introduction

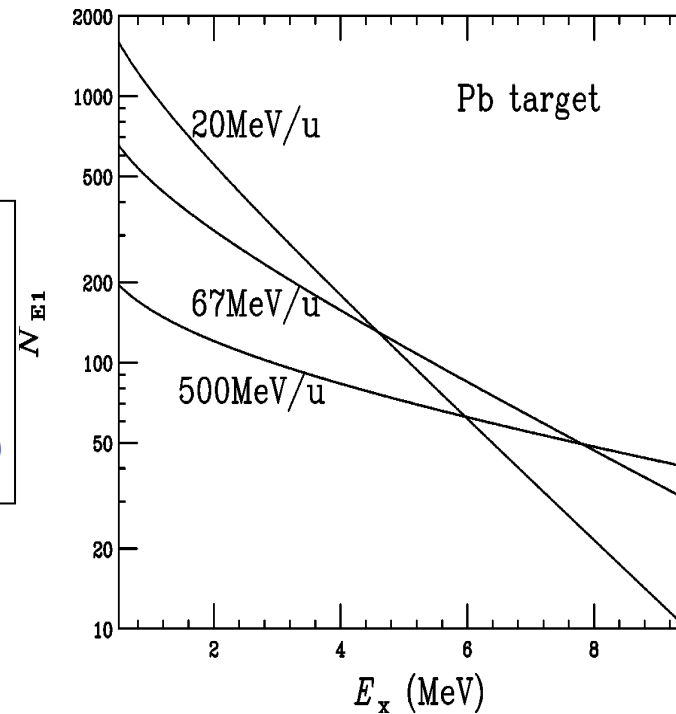
# Coulomb Dissociation



## Equivalent Photon Method

$$\frac{d\sigma_{CD}}{dE_x} = \frac{16\pi^3}{9\hbar c} N_{E1}(E_x) \frac{dB(E1)}{dE_x}$$

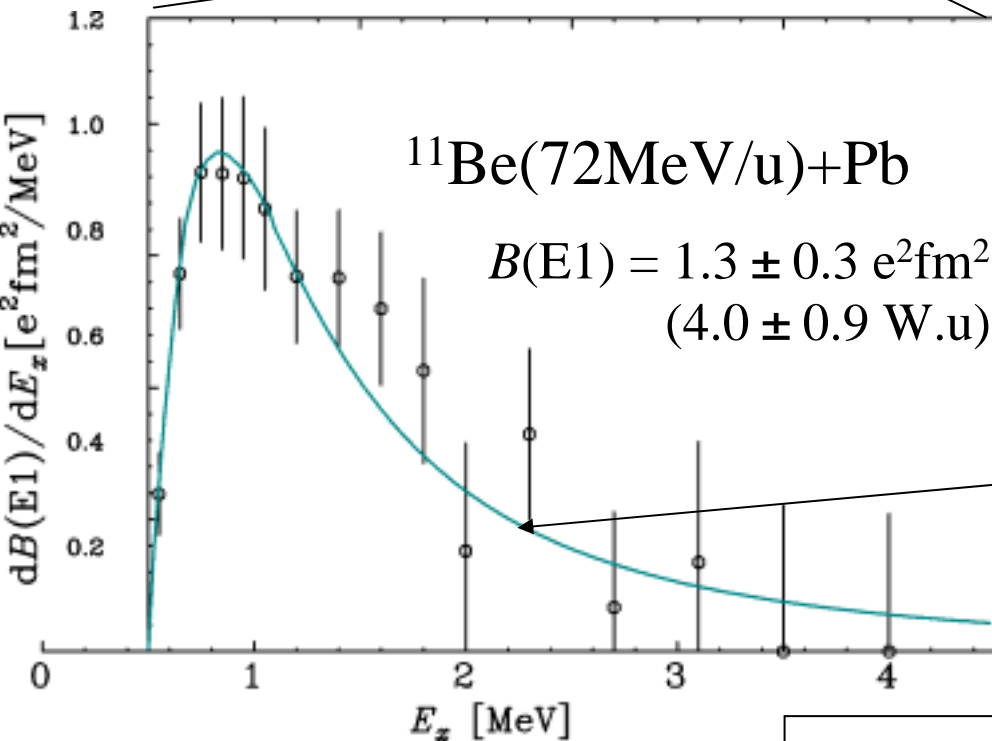
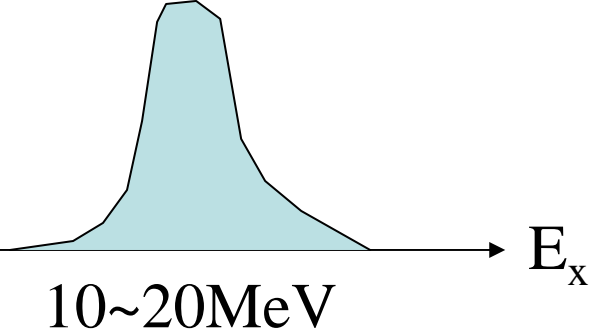
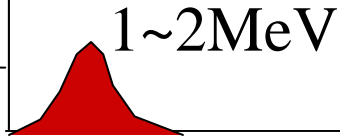
Cross section = (Photon Number) x (Transition Probability)



# $^{11}\text{Be}$ – The Classical case

$S_n = 504 \text{ keV}$

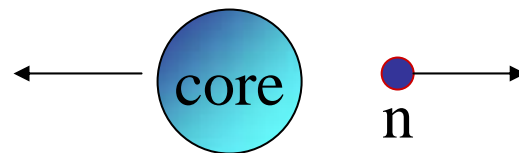
$$\frac{dB(E1)}{dE_x}$$



@RIKEN

T.Nakamura *et al.*,  
PLB 331,296(1994)

Direct Breakup



$$\frac{dB(E1)}{dE_x} \propto \left| \langle \mathbf{q} | \frac{Z}{A} r Y_{1m}^1 | \Phi_{gs} \rangle \right|^2$$

$$\Phi_{gs} \propto \frac{e^{-r/\lambda}}{r} \Rightarrow B(E1) \propto 1/S_n \quad E_x(\text{peak}) = \frac{8}{5} S_n$$

# Spectroscopic Significance

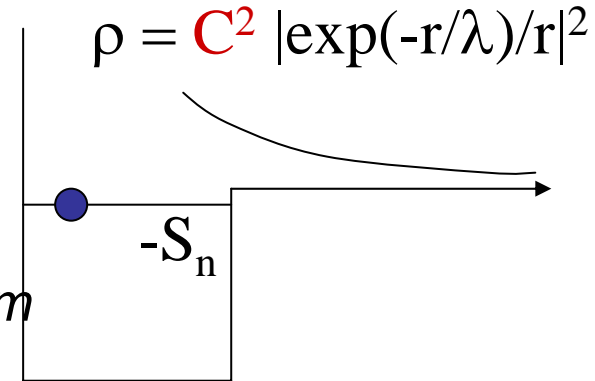
Direct Breakup Mechanism

$$\frac{dB(E1)}{dE_x} \propto \left| \langle \exp(iqr) \left| \frac{Z}{A} r Y^1_m \right| \Phi_{gs} \rangle \right|^2$$

$$\propto C^2 \left| \langle \exp(iqr) \left| \frac{Z}{A} r Y^1_m \right| \frac{\exp(-r/\lambda)}{r} \rangle \right|^2$$

Low-lying E1 Strength

Fourier Transform



Halo State

**B(E1) @E~1MeV**

**Exclusively Sensitive to the Halo State**

ANC( $C^2$ )->spectroscopic factor  $\alpha^2$

$$| \Phi_{gs} (1/2^+) \rangle = \alpha | ^{10}\text{Be}(0^+) \otimes 2s_{1/2} \rangle + \beta | ^{10}\text{Be}(2^+) \otimes 1d_{5/2} \rangle + ..$$

$^{11}\text{Be}(\text{g.s.})$

Halo State

$\alpha^2, \beta^2$  : Spectroscopic factor

$$\alpha^2 = 0.8 \pm 0.2 \text{ (1994 data)}$$

$$\text{c.f. } \alpha^2 = 0.77 \text{ } ^{10}\text{Be}(d,p)^{11}\text{Be}$$

# Remaining Issues on Coulomb Dissociation?

Direct Breakup  $\frac{dB(E1)}{dE_x} \propto \left| \langle \mathbf{q} \mid \frac{Z}{A} r Y^1_m \mid \Phi_{gs} \rangle \right|^2$

Equivalent Photon Method----- 1<sup>st</sup> Order Perturbation

- ① Higher Order Effect
- ② Distorted Wave (Final State)
- ③ Nuclear Breakup Contribution

--*How To subtract the Nuclear Contribution?*

M.A. Nagarajan, C.H.Dasso, S.M.Lenzi, A. Vitturi PLB503,65(2001).

C.H. Dasso, S.M. Lenzi, and A. Vitturi PRC59,539(1999).

S. Typel and R.Shyam PRC64, 024605(2001).

G.Baur, C.A.Bertulani, D.M.Kalassa, NPA550, 527(1992)

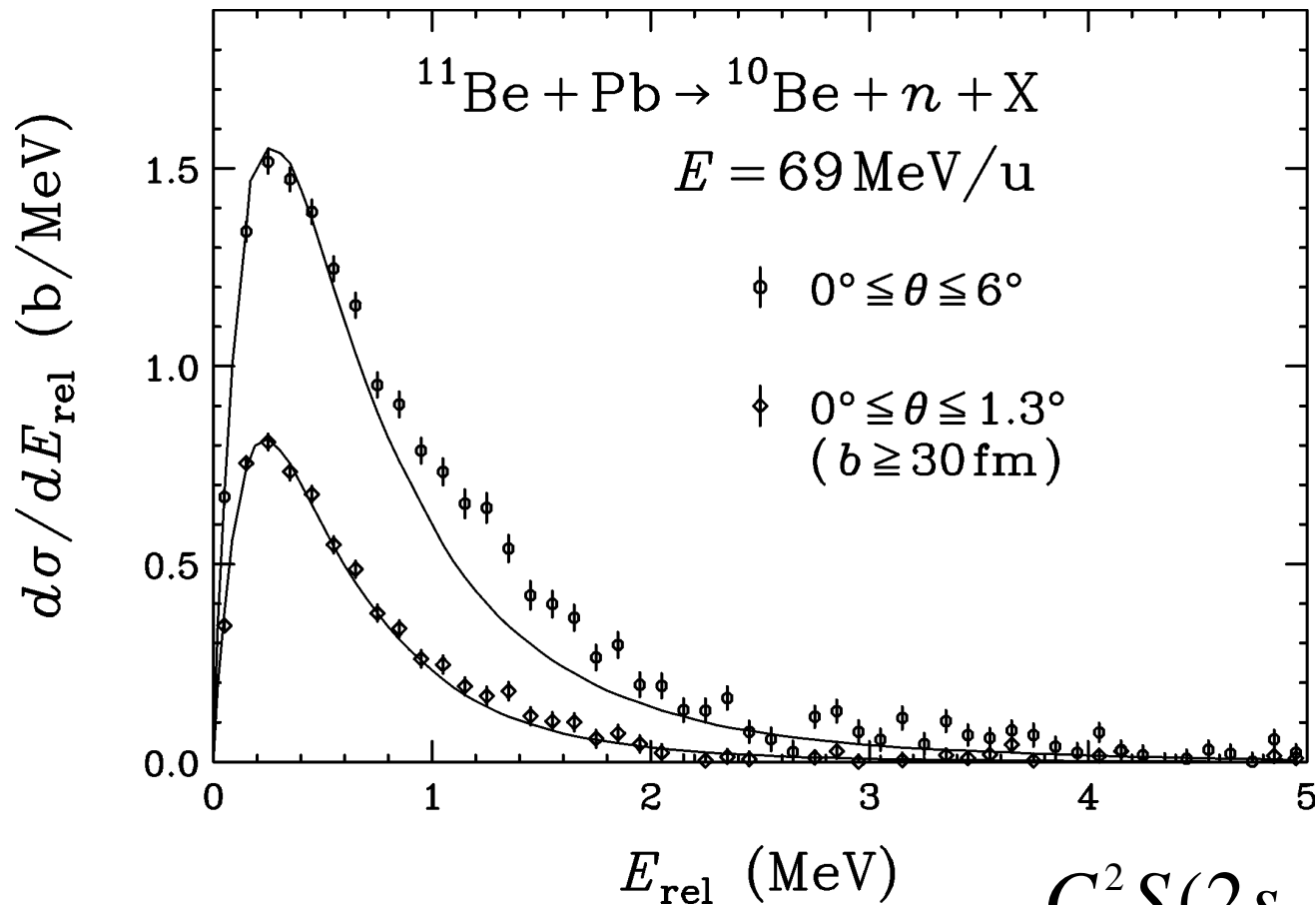
H.Esbensen, G.F.Bertsch, C.A.Bertulani ,NPA581,107 (1995) .

J.Margueron, A. Bonaccorso, and D.M.Brink, NPA720,337(2003); NPA703,105(2002).

I.J.Thompson and J.A. Tostevin NPA690,294c(2001).

S. Typel and G. Baur PRC64, 024601(2001)

# Relative Energy Spectrum

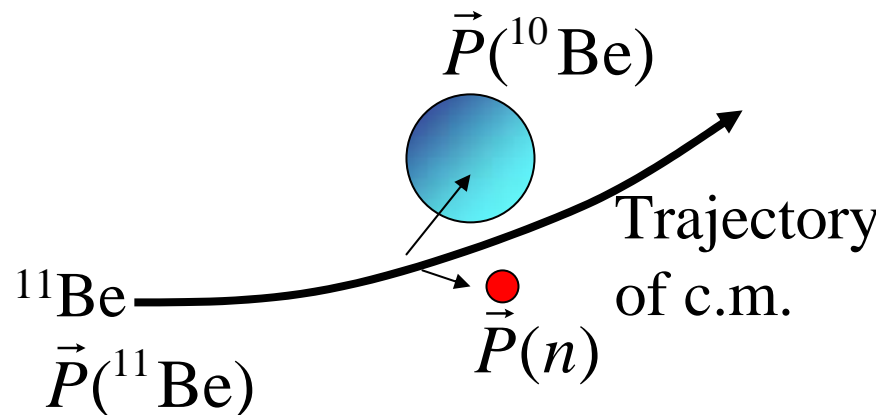
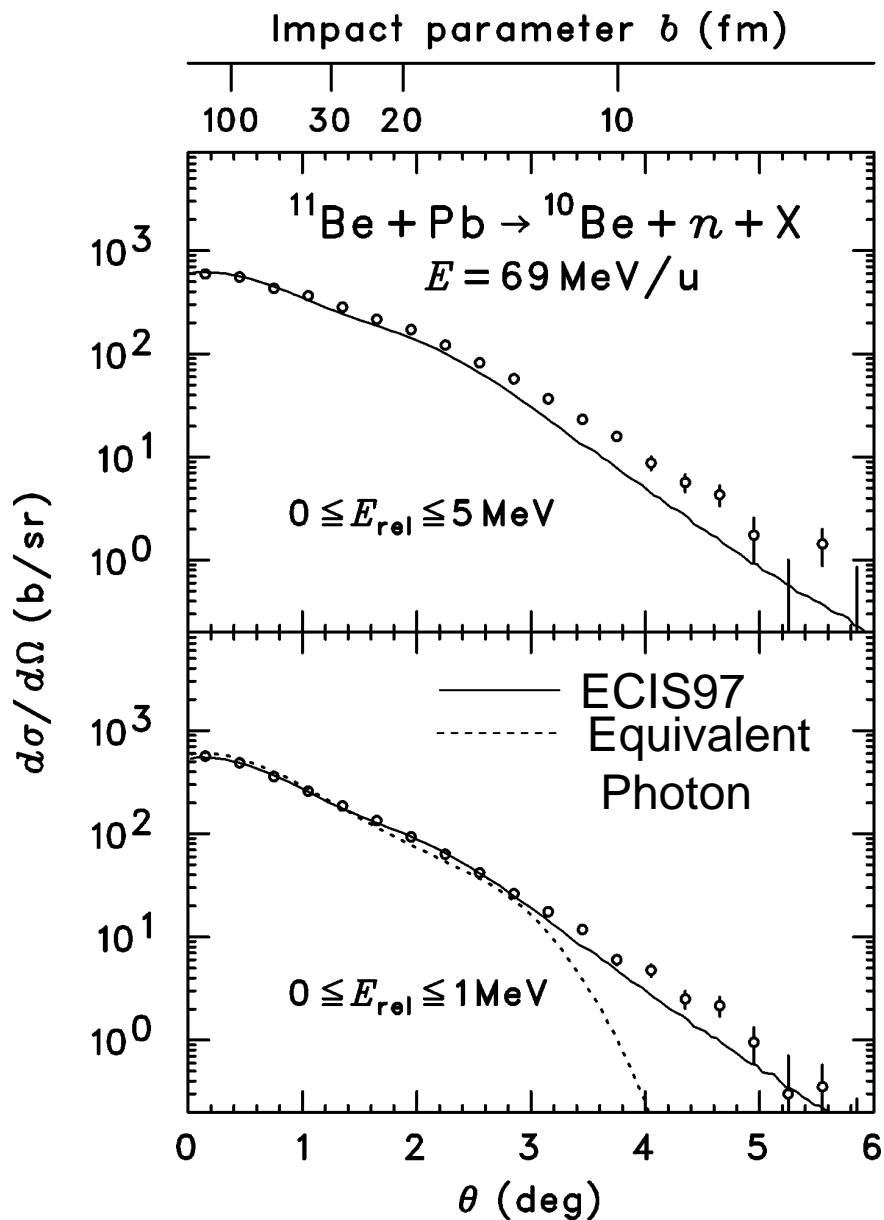


$$C^2S(2s_{1/2}) = 0.72 \pm 0.04$$

$$\sigma(\text{Pb}) = 1.79 \pm 0.02 \text{ (b)}$$

$$\sigma(\text{Pb}; \text{Coul}) = 1.51 \pm 0.02 \text{ (b)}$$

# Angular Distribution of $^{10}\text{Be}+n$ c.m. System

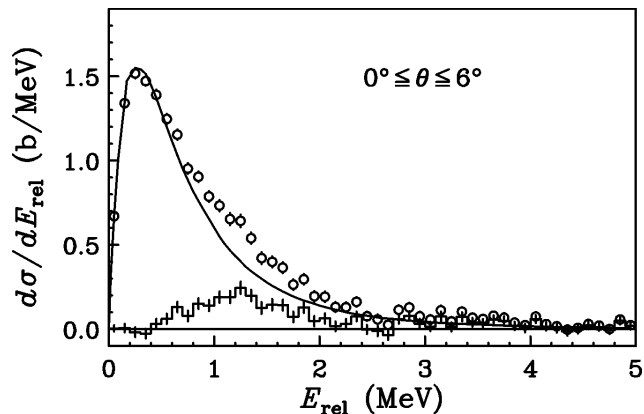
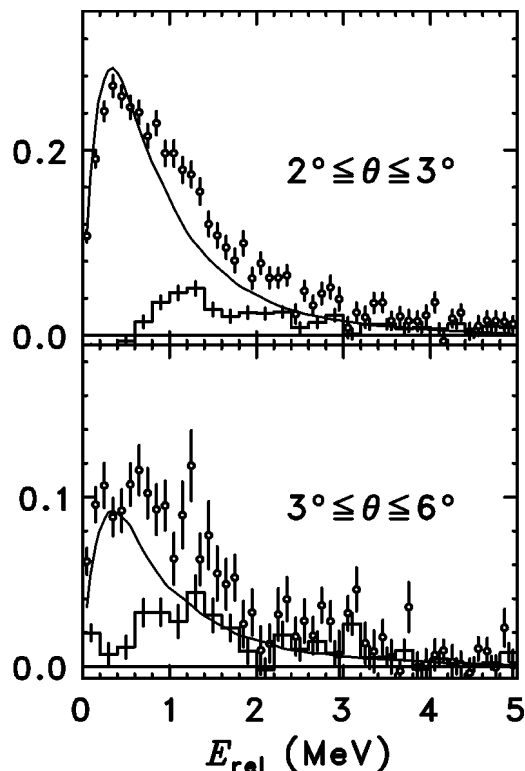
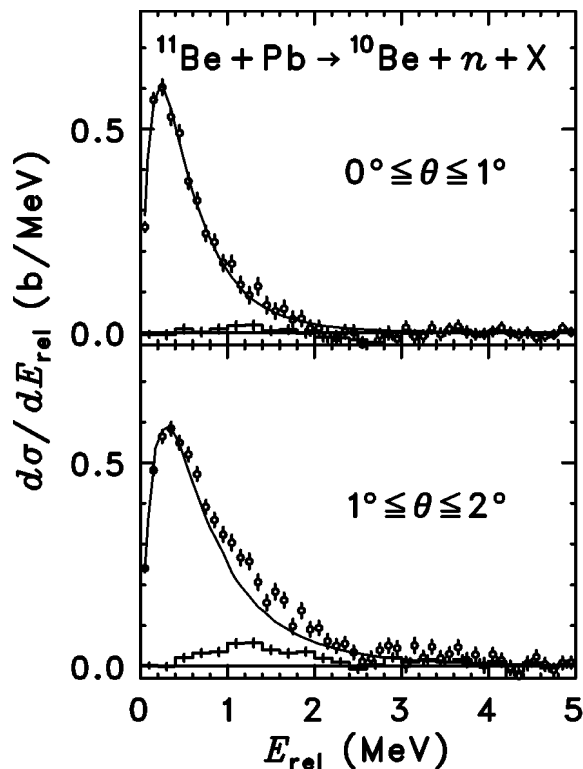


$$b = a \cot(\theta/2)$$

Negligible Higher Order Effects  
 and Nuclear Contribution  
 for  $b > 30 \text{ fm}$  ( $\theta < 1.3 \text{ deg}$ )



# Nuclear Contribution & Higher Order effect



Nuclear contribution and/or Higher order effects  $\frac{280 \text{ mb}}{1.79 \text{ b}} = 15.6\%$

For the whole angular range

$$\frac{\sigma(\text{Pb}; \text{nucl})}{\sigma(\text{C}; \text{nucl})} = \frac{280 \text{ mb}}{81 \text{ mb}} = 3.5 > 1.8 (r_{\text{sum}} \text{ ratio})$$

# Sum Rule

## Energy Weighted Sum Rule (TRK Sum Rule)

$$\int \sigma_{\gamma}(E_{\gamma}) dE_{\gamma} = \int \frac{16\pi^3}{9\hbar c} E_x \frac{dB(E1)}{dE_x} dE_x = 60 \frac{NZ}{A} \text{ (MeV} \cdot \text{mb)}$$

153 MeVmb for  $^{11}\text{Be}$

## Cluster sum rule Y.Alhassid, M.Gai, and G.F.Bertsch PRL49,1482(1982)

$$\text{Sum} = 60 \frac{NZ}{A} - 60 \frac{N_c Z_c}{A_c} = 8.73 \text{ MeV} \cdot \text{mb} \quad \text{For } ^{11}\text{Be}$$

Experiment ( $E_x < 4.5 \text{ MeV}$ )

$$\text{Sum} = 5.69 \pm 0.45 \text{ MeV} \cdot \text{mb} = 3.7(2) \% \text{ of TRK Sum} = \mathbf{65(5) \%} \text{ of Cluster Sum} \\ \sim \mathbf{\text{Spectroscopic Factor}}$$

## Non Energy Weighted Cluster Sum Rule H.Esbensen et al., NPA542,310(1992)

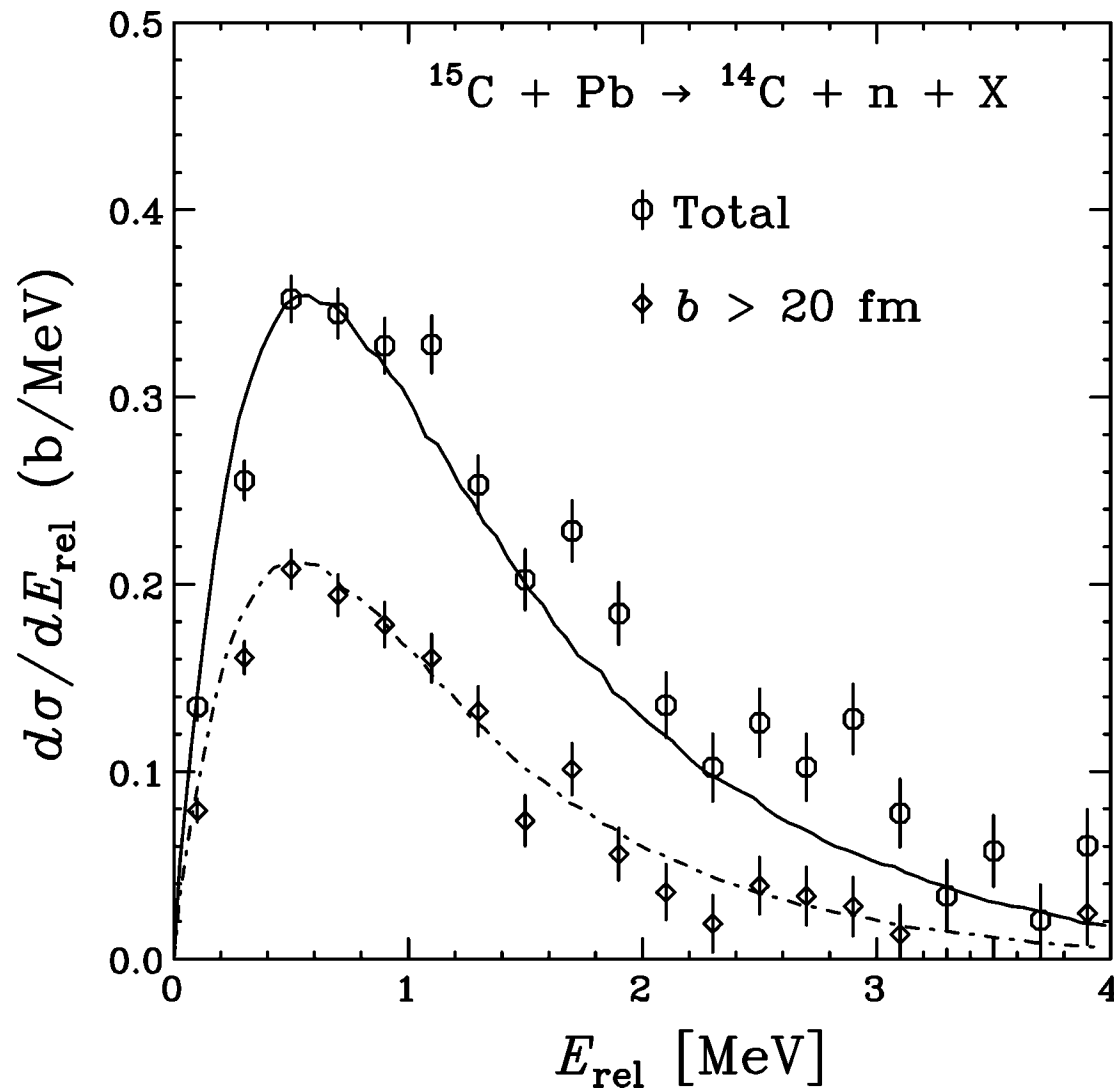
$$B(E1) = \int_0^{\infty} \frac{dB(E1)}{dE_x} dE_x = \frac{3}{4\pi} \left( \frac{Ze}{A} \right)^2 \langle r^2 \rangle$$

$$\text{Experiment: } B(E1) = 1.10 \pm 0.08 e^2 \text{fm}^2 \implies \sqrt{\langle r^2 \rangle} = 5.37 \pm 0.20 \text{fm}$$

# Application: Coulomb Dissociations of $^{15}\text{C}$

$$S_n = 1.218 \text{ MeV}$$

$$^{15}\text{C}(\text{g.s.}) = \alpha | ^{14}\text{C}(0^+) \otimes 2s_{1/2} \rangle + \beta | ^{14}\text{C}(2^+) \otimes 1d_{5/2} \rangle$$



$^{15}\text{C} + \text{Pb} @ 68 \text{ MeV/u}$

$$\alpha^2 = 0.74(4)$$

$$r_0 = 1.25 \text{ fm}$$

$$a = 0.65 \text{ fm}$$

Consistent with GSI data (0.73)  
 (D. Pramanik et al. PLB 551, 63  
 (2003))

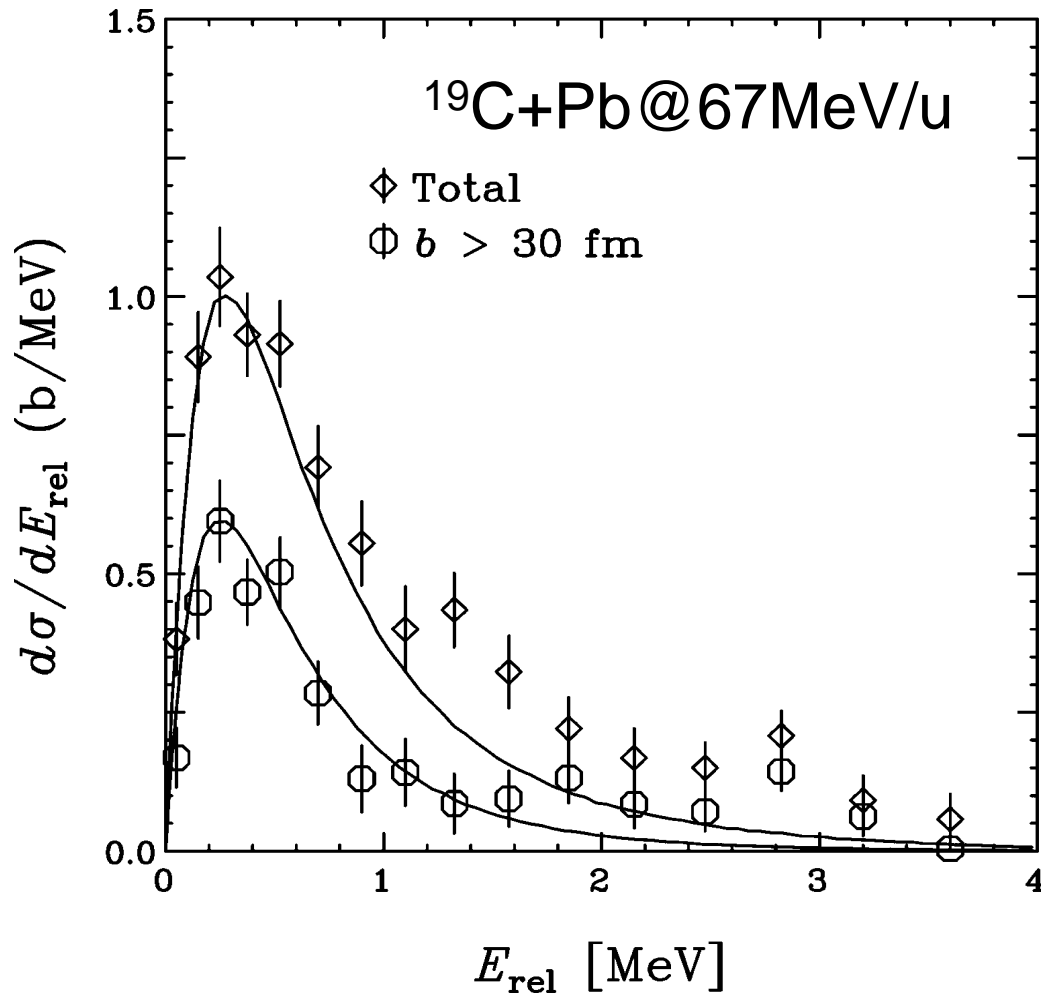
But not with MSU data  
 A. Horvath et al., APJ (2001)  
 Beer et al. ApJ 387, 258 (1992)

# Coulomb Dissociations of $^{19}\text{C}$

$^{19}\text{C}$   $S_n=0.53\text{MeV}$

T.Nakamura *et al.*,  
PRL. 83, 1112 (1999)

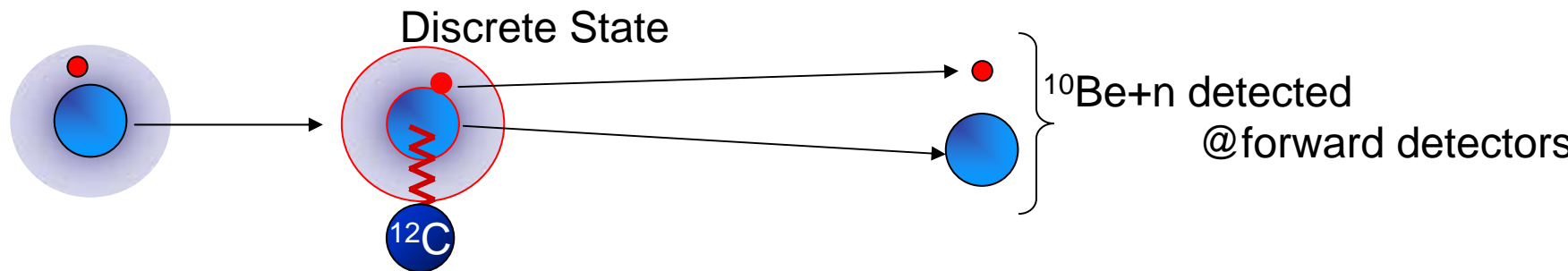
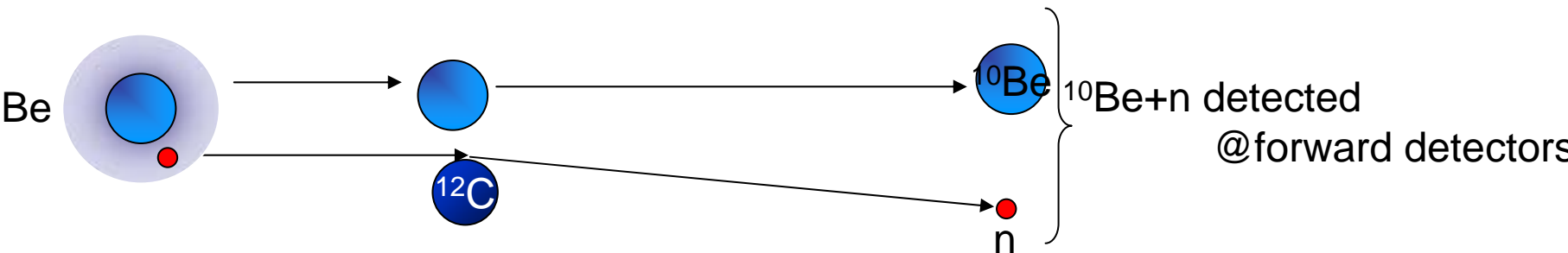
$$^{19}\text{C}(\text{g.s.}) = \alpha | \underline{^{18}\text{C}(0^+) \otimes 2s_{1/2}} \rangle + \beta | ^{18}\text{C}(2^+) \otimes 1d_{5/2} \rangle$$



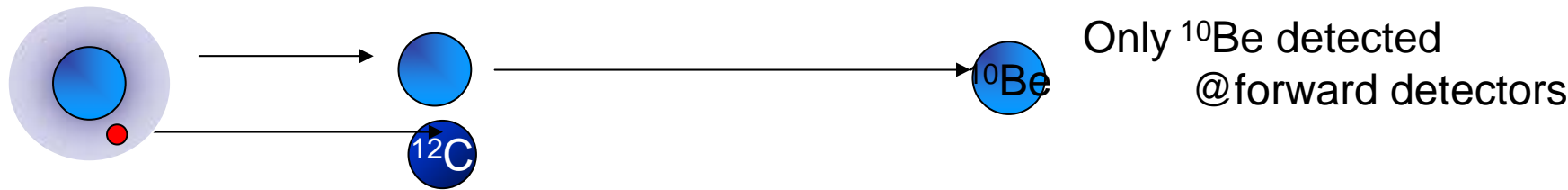
$$\alpha^2=0.67$$

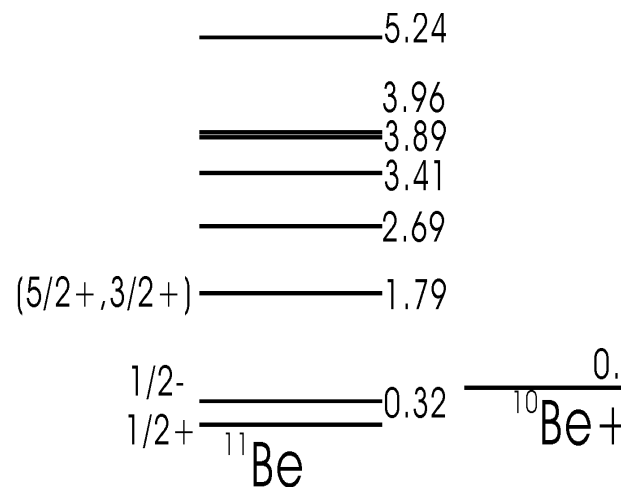
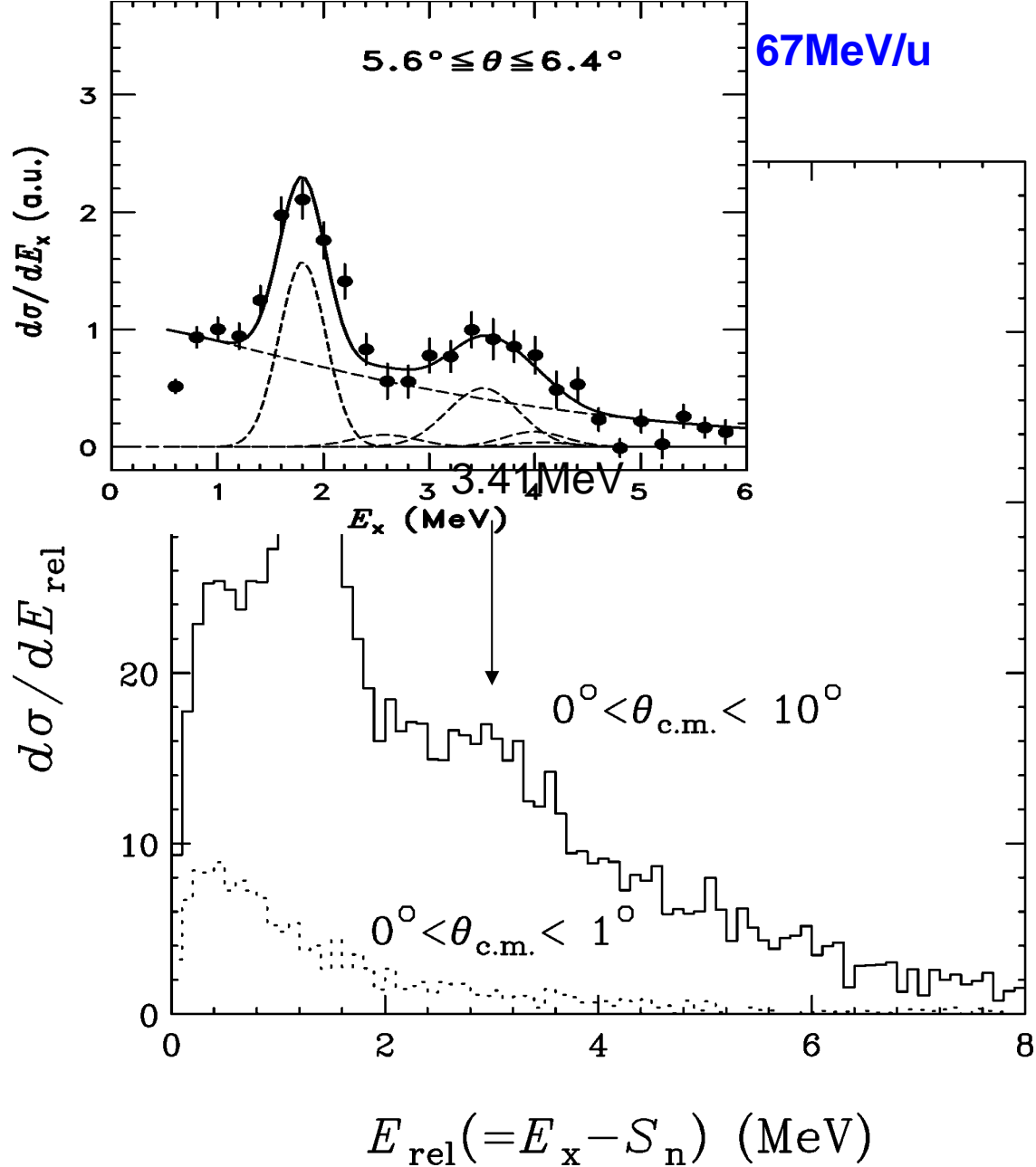
## 2 Nuclear Breakup of $^{11}\text{Be}$

### Diffractive Breakup (Elastic Breakup)



### 1n-stripping (knockout) reaction

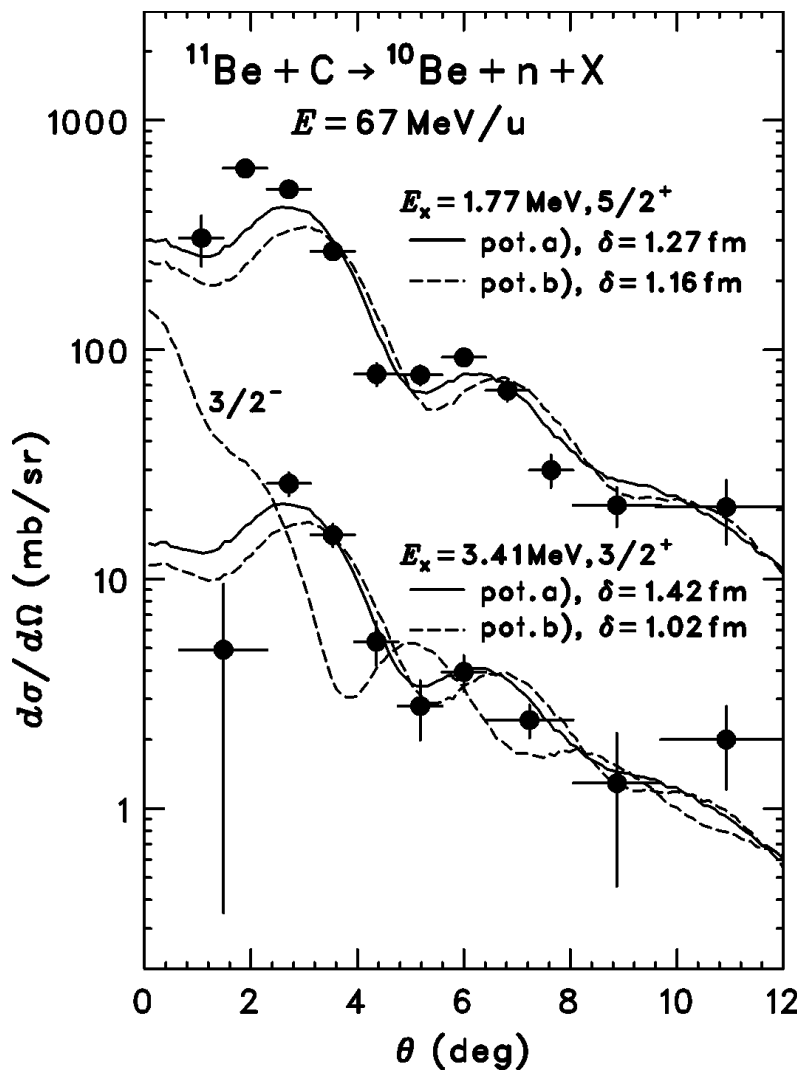




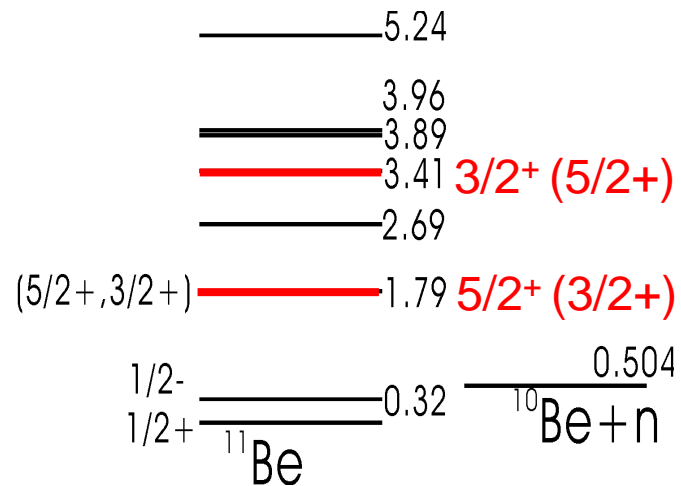
Known Levels

# $^{11}\text{Be} + \text{C}$ - Angular Distribution

$^{11}\text{Be} + \text{C}$  @ 67 MeV/u



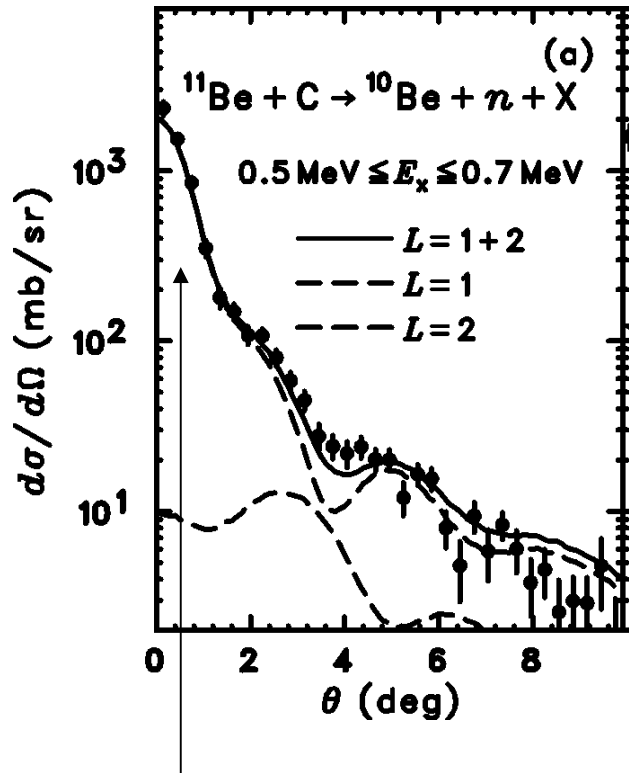
$\Delta L=2$  Transition @  $E_x=1.79 \text{ MeV}$   
 @  $E_x=3.41 \text{ MeV}$



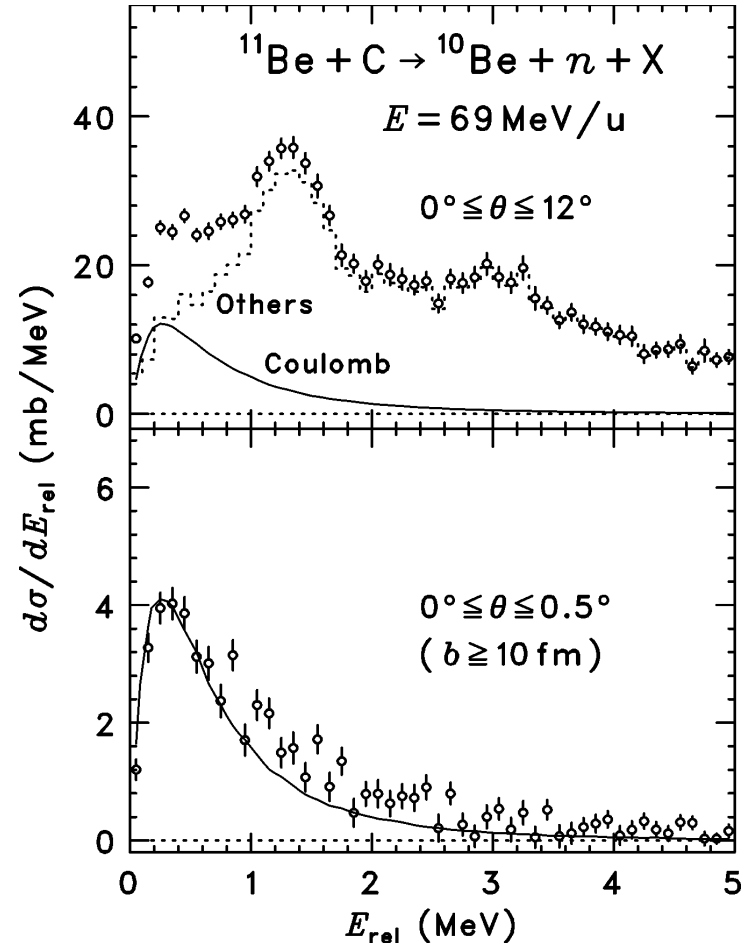
Potential a)  $^{11}\text{Be} + ^{12}\text{C}$  @ 48 MeV/u

b)  $^{12}\text{C} + ^{12}\text{C}$  @ 84 MeV/u

# Coulomb Contribution in C target data



Strong Coulomb Contribution  
 (Absolute value is consistent with  
 Coulomb contribution at Pb target)

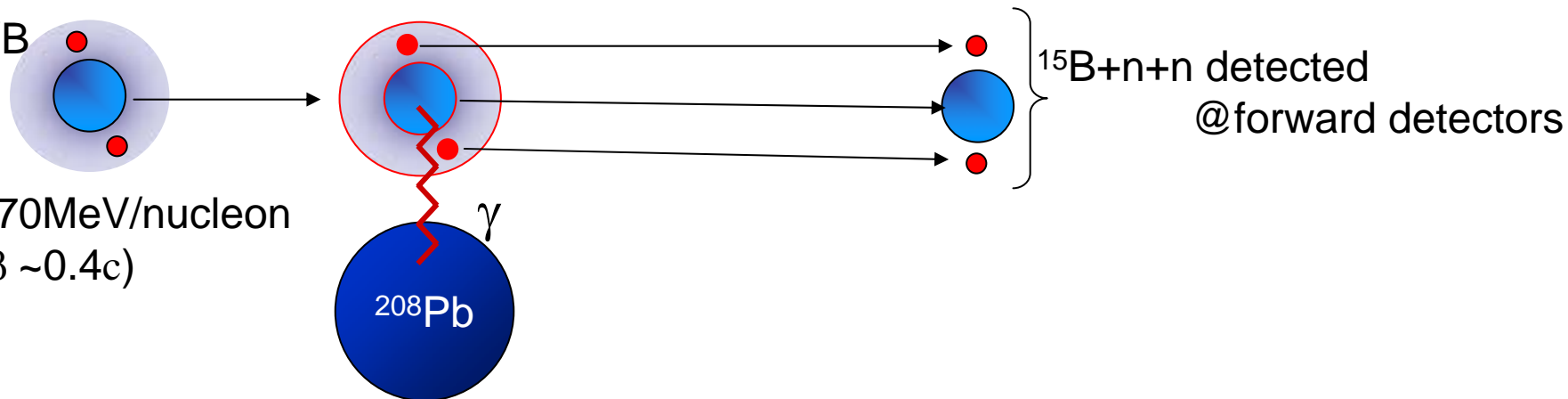


Direct Coulomb Breakup  
 even for C target

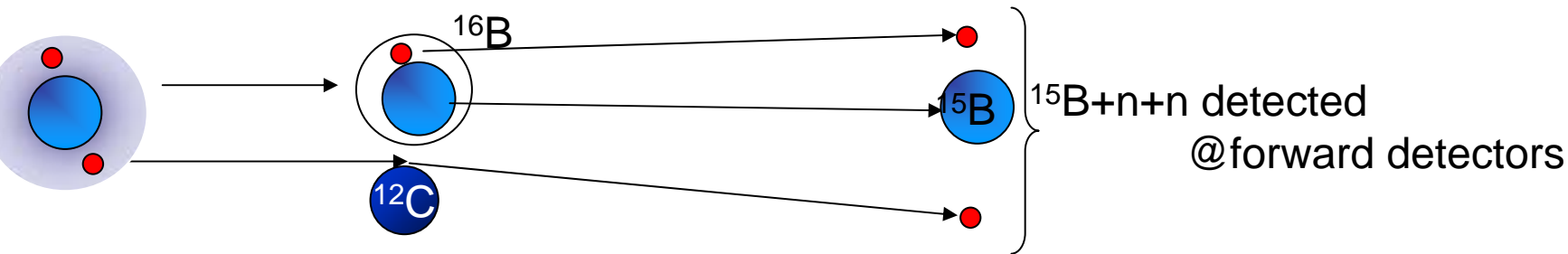
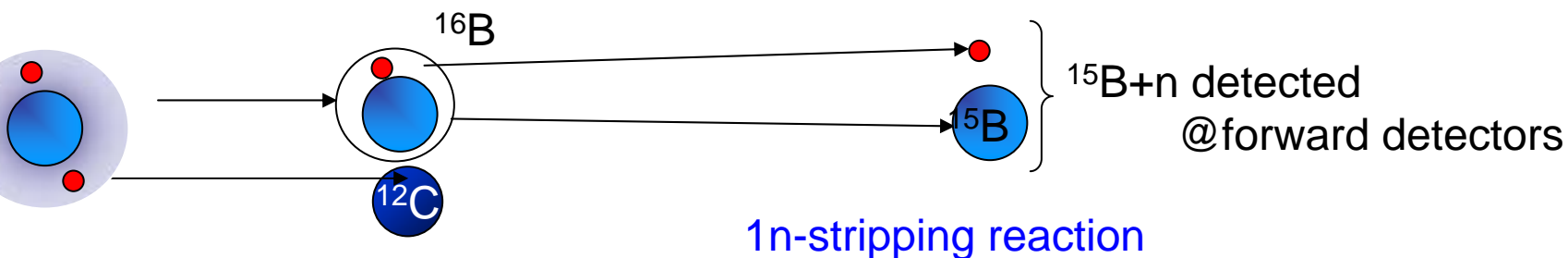


# 3 Breakup of 2-n Halo Nuclei $^{11}\text{Li}$ , $^{14}\text{Be}$ , $^{17}\text{B}$

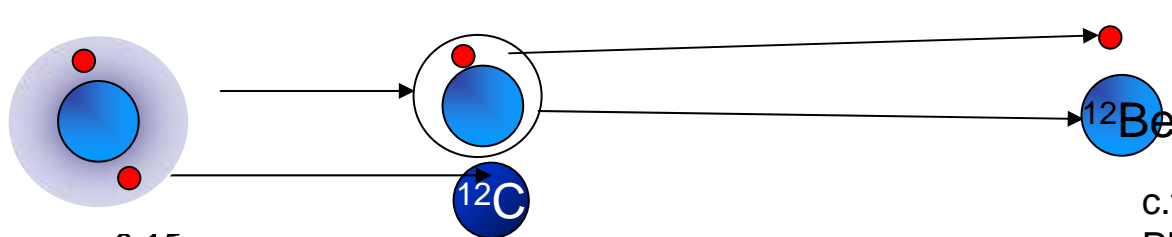
## Coulomb Breakup of two-neutron halo nuclei



## Nuclear Breakup of two-neutron halo nuclei



# $^{12}\text{Be}+n$ ( $^{13}\text{Be}$ ) Relative Energy Spectrum



S-wave scattering state

c.f. G.F. Bertsch, K. Hencken, H.Esbensen  
PRC57, 1366(1998)

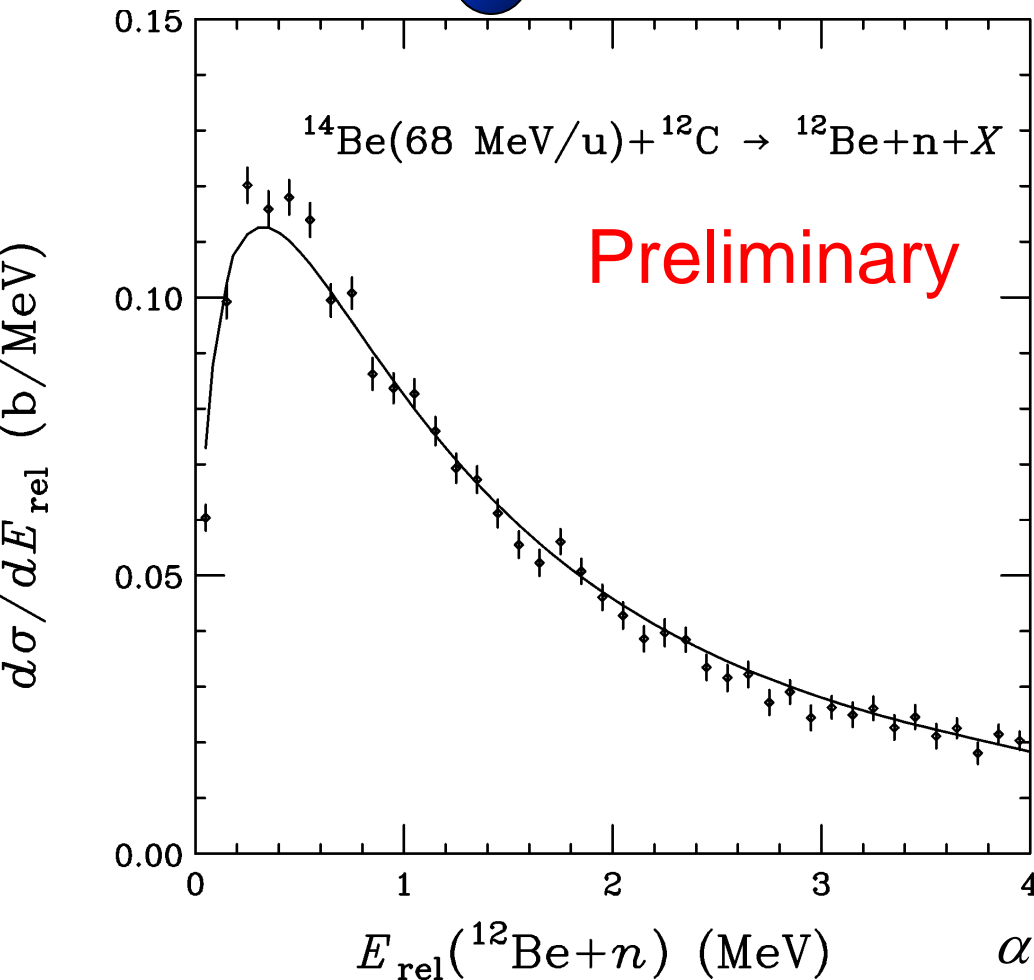
$$\frac{d\sigma}{dE_{rel}} \propto \left| \int d^3r \psi_k^*(r) \Psi_0(r) \right|^2 k$$

Initial:  $^{14}\text{Be}$   $\Psi_0(r) \propto \frac{\exp(-\alpha r)}{r}$

Final: s-wave  $\psi_k(r) \propto \frac{\sin(kr + \delta)}{kr}$

$$k \cot \delta = -\frac{1}{a} + \frac{1}{2} r_e k^2$$

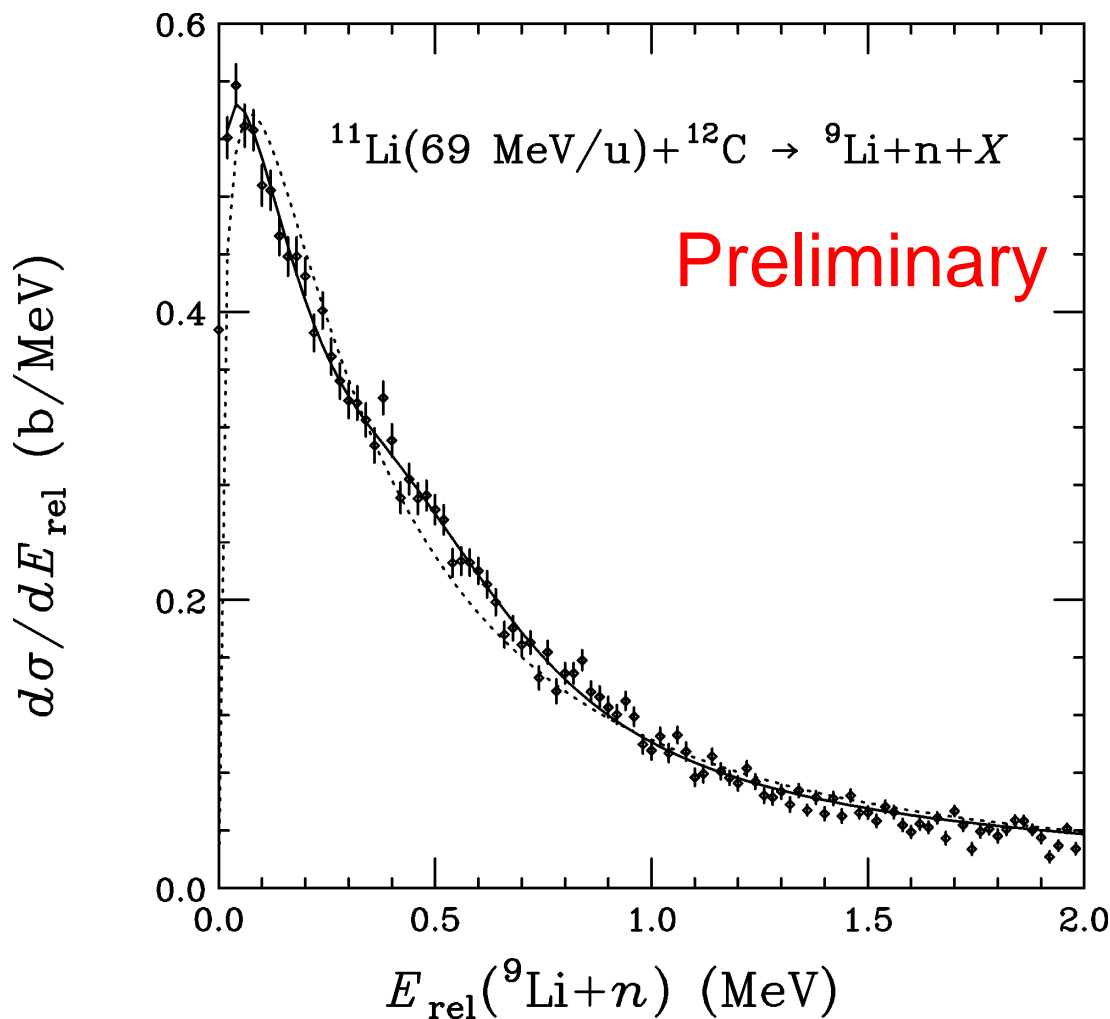
$$\left\{ \begin{array}{l} a = -3.5(5) \text{ fm} \\ \alpha = 0.26(2) \text{ fm}^{-1} \\ r_e = 0.8(3) \text{ fm} \end{array} \right.$$



$$\alpha = \sqrt{2\mu S_{eff}} / \hbar \quad \text{Small effective range}$$

$$S_{eff} = 1.5 \text{ MeV}$$

# ${}^9\text{Li}+n$ ( ${}^{10}\text{Li}$ ) Relative Energy Spectrum



S-wave scattering state  
+ p-wave resonance

S-wave

$$\begin{cases} a = -26.2(1.4) \text{ fm} \\ \alpha = 0.16(1) \text{ fm}^{-1} \\ r_e = 5.6(4) \text{ fm} \end{cases}$$

$$\alpha = \sqrt{2\mu S_{\text{eff}}} / \hbar$$

$$S_{\text{eff}} = 0.6 \text{ MeV}$$

p-wave

$$\frac{d\sigma}{dE_{\text{rel}}} \propto \frac{\Gamma}{(E - E_R)^2 + \Gamma^2 / 4}$$

$$\Gamma = 2P_l \gamma^2 \quad P_{l=1}(kr) = \frac{(kr)^3}{1 + (kr)^2}$$

$$E_R = 0.52(2) \text{ MeV}$$

$$\gamma^2 = 0.36(7) \text{ MeV}$$

c.f. p-wave resonance:  $\leftarrow$   
B. Young et al. 0.54(6) MeV

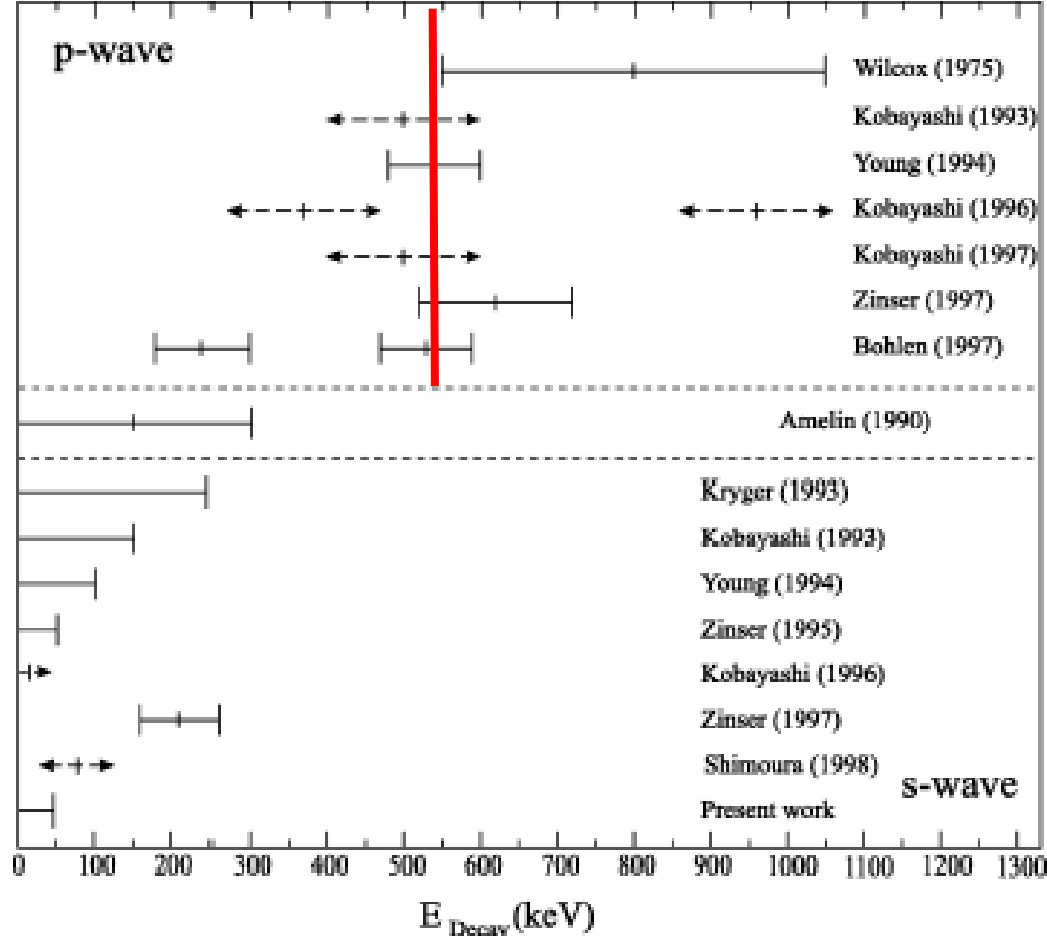
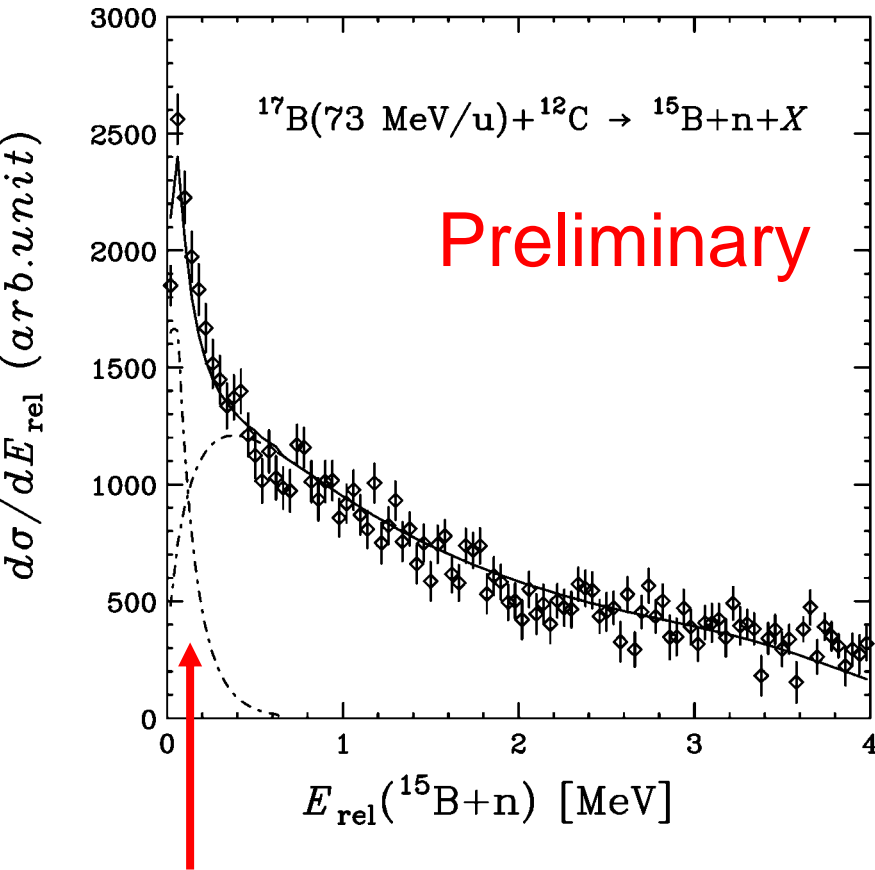


FIG. 9. Comparison of experimental results for  $p$ - and  $s$ -wave states. The  $s$ -wave states are presented in terms of apparent peak energies.

**Phys. Rev. C 59, 111–117 (1999).**  
**M.Thoennessen**

# $^{16}\text{B}$ ( $^{15}\text{B}+n$ )

(S.Sugimoto's analysis)



$$E_R = 60 \text{ keV}$$

$$\gamma^2 = 91(9) \text{ keV}$$

c.f.

Eur. Phys. J. A7, 451 (2000)  $E_{\text{rel}} = 40 \text{ keV}$

*Assumed*

**s-wave scattering state**

$$a = -0.0025 \pm 0.17 \text{ fm}$$

$$\alpha = 0.206 \pm 0.002 \text{ fm}^{-1}$$

$$r_e = 4.2 \pm 6.6 \text{ fm}$$

**+**

**d-wave resonance**

$$\frac{d\sigma}{dE_{\text{rel}}} \propto \frac{\Gamma}{(E - E_R)^2 + \Gamma^2 / 4}$$

$$\Gamma = 2P_{l=2}\gamma^2$$

$$P_{l=2}(kr) = \frac{(kr)^5}{9 + 3(kr)^2 + (kr)^4}$$

$$E_R = 60 \text{ keV}$$

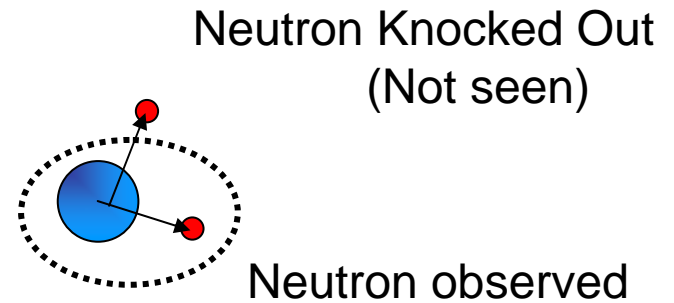
$$\gamma^2 = 91(9) \text{ keV}$$

# S-wave scattering analysis

$$\frac{d\sigma}{dE_{rel}} \propto \left| \int d^3r \psi_k^*(r) \Psi_0(r) \right|^2 k$$

Initial:  $^{14}\text{Be}$   $\Psi_0(r) \propto \frac{\exp(-\alpha r)}{r}$

Final: s-wave  $\psi_k(r) \propto \frac{\sin(kr + \delta)}{kr}$



Things to be investigated:

- Amplitude should be related to the Spectroscopic factor?
- Can this be used to study the phase shift of halo nuclei?
- $\overrightarrow{P}(^{13}\text{Be})$  should have information of the Spectroscopic factor



1

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