

**Tsironis *et al.* Reply:** The numerical calculations presented in Ref. 1 were aimed at bridging *two exact limits within the Fokker-Planck (FP) approximation*. In the limit of short correlation times  $\tau$ , this approximation reduces to a standard stationary FP equation thereby recovering standard results with increasing accuracy as the intensity of noise decreases,<sup>2</sup> whereas in the large- $\tau$  region, the slope of the logarithm of the mean first-passage time (MFPT) as a function of  $\tau$  was shown to coincide with exact predictions.<sup>1,3</sup> The bridging of the two extremes was accomplished in the context of a local linearization (LL) theory which is locally exact and satisfies simultaneously the constraints at short and long  $\tau$ . The new Fokker-Planck-type theory retains the non-stationary character of the process, which is essential for the region  $\tau > \tau_c$  ( $\alpha\tau_c \equiv 1$ ), and circumvents the appearance of either negative diffusion coefficients or that of negative friction parameters. It is noteworthy to point out that the approach referred in the previous Comment<sup>4</sup> belongs in the latter category (Ref. 3 of Ref. 4), which has the additional shortcoming of not providing exact dynamical properties.

The LL theory is a FP approximation whose equilibrium distribution, even in the unstable case, leads, in the intermediate- $\tau$  region, to quantitative disagreement with

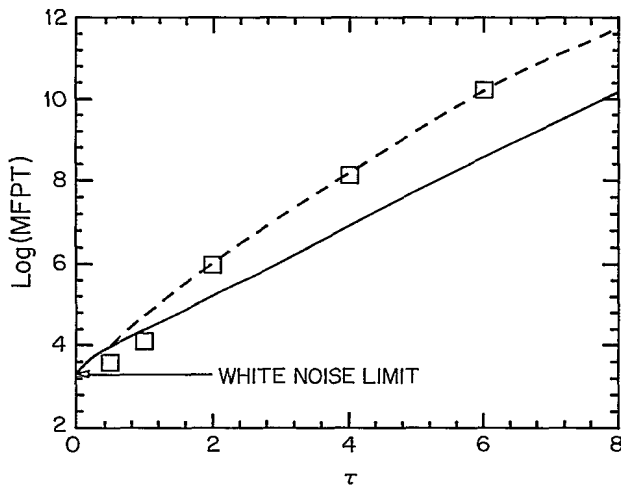


FIG. 1. The TG relaxation time  $T(\tau)$  (solid line) is compared to the result of numerical simulations (dashed line) and to the improved TG theory (Ref. 7) (squares) obtained by averaging the expression in p. 8 of Ref. 1 over the statistical distribution of  $\xi_c$ , which marks the actual noise value at which the transition to the other well takes place. In Refs. 6 and 7 it is shown that for  $\tau \rightarrow \infty$  this expression tends to the above-mentioned TG formula. The digital simulation has been carried out with diffusion coefficient  $D=0.1$  (Ref. 7).

digital simulations.<sup>5</sup> When studying escape processes, these kinds of discrepancies are enhanced exponentially, without conflicting, however, with the constraint of recovering the TG prediction<sup>1</sup> for  $\tau \rightarrow \infty$ . This asymptotic agreement was reestablished recently by de la Rubia *et al.*<sup>6</sup> who showed that although the TG prediction on the MFPT is smaller than the true one for large but finite  $\tau$ 's because barrier crossings can occur at noise values other than the critical one, the TG prediction is recovered for  $\tau \rightarrow \infty$  [Eq. (13) of Ref. 6]. Along these lines, a further improved TG theory has been shown by Mannella and Palleschi<sup>7</sup> to lead to a very accurate *quantitative* agreement with digital simulation results (Fig. 1). We thus conclude that the TG theory does indeed provide a reliable bridging between two exact limits and is a proper reference point for ongoing theoretical work.

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